

Table 1: Number of significant windows differences around the start-task time.

Time	significant difference
-2s to 0s and 0s to 2s	13
0s to 2s and 2s to 4s	21
2s to 4s and 4s to 6s	18
4s to 6s and 6s to 8s	14
6s to 8s and 8s to 10s	20
8s to 10s and 10s to 12s	26

Table 2: Number of significant windows differences around the end-task time.

Time	significant difference
-2s to 0s and 0s to 2s	13
0s to 2s and 2s to 4s	20
2s to 4s and 4s to 6s	23
4s to 6s and 6s to 8s	19
6s to 8s and 8s to 10s	18
8s to 10s and 10s to 12s	20

ing C4 in the 10–20 system. In the estimation, the task start time is set to 0 s, and the Mann–Whitney U test is performed in every 2-s window by shifting the window from –2 s to 12 s. Next, the after-task rest start time was set to 0 s, and then the U test was performed as above. Tables 1 and 2 show the number of significant differences for task-start and task-end analysis at a significance level of 1%. These tables show an estimated 2-s delay, because there are a number of significant differences between 0 and 2 s and between 2 and 4 s from the previous window.

4. Classification Algorithm

4.1. ELM

ELM is a learning algorithm for single-hidden-layer feedforward neural networks (SLFNs) proposed by Huang et al. [3]. Figure 2 shows the structure of ELM. The algorithm is as follows. Assume a training set, activation function $g(x)$, and hidden node number I . An input weight w_i and bias b_i are randomly generated, and the hidden layer output matrix \mathbf{H} is calculated as

$$\mathbf{H} = \begin{bmatrix} g(w_1x_1 + b_1) & \cdots & g(w_Ix_1 + b_I) \\ \vdots & \ddots & \vdots \\ g(w_1x_N + b_1) & \cdots & g(w_Ix_N + b_I) \end{bmatrix}, \quad (1)$$

where

$$g(a) = \frac{1}{1 + e^{-a}}. \quad (2)$$

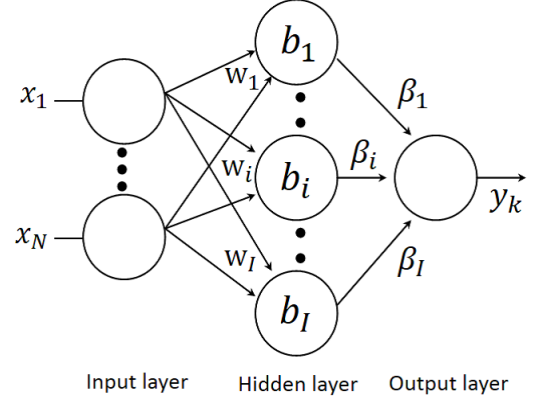


Figure 2: Structure of ELM.

Next, calculate the output weight β as

$$\beta = \mathbf{H}^+ \times T, \quad (3)$$

where T is the training data set and \mathbf{H}^+ denotes the pseudo-inverse matrix of \mathbf{H} . Finally, we calculate the output value y as

$$y = \mathbf{H}\beta. \quad (4)$$

4.2. SVM

SVM is a classifier proposed by Vapnik et al. [4]. A kernel trick can be easily applied to SVM. The decision function of SVM is

$$D(x) = \sum_{i \in S} \alpha_i y_i K(x_i, x) + b, \quad (5)$$

where

$$b = y_j - \sum_{i \in S} \alpha_i y_i K(x_i, x_j). \quad (6)$$

Here, α , y and $K(x_i, x)$ are a Lagrange multiplier, output training data, and a kernel function, respectively[5]. In this, α is obtained by solving the following optimization problem:

$$\max Q(\alpha) = \sum_{i=1}^M \alpha_i - \frac{1}{2} \sum_{i,j=1}^M \alpha_i \alpha_j y_i y_j K(x_i, x_j), \quad (7)$$

$$\text{s.t. } \sum_{i=1}^M y_i \alpha_i = 0, \quad (0 < \alpha_i < C). \quad (8)$$

4.3. SVR

SVR is a modified SVM algorithm adapted for application to regression problems [5][6][7]. The decision function of SVR is

$$f(x) = \sum_{i=1}^m (\alpha_i - \alpha_i^*) K(x_i, x) + b, \quad (9)$$

where

$$b = y_i - w^\top \phi(x_i) - \varepsilon \quad (0 < \alpha_i < C), \quad (10)$$

$$b = y_i - w^\top \phi(x_i) + \varepsilon \quad (0 < \alpha_i^* < C). \quad (11)$$

Here, α_i^* , w , ϕ , and ε are a Lagrange multiplier, a coefficient vector, a mapping function, and the width of a ε tube, respectively. The ε tube is used to reduce error close to the regression curve, with the error defined as

$$E(r) = \begin{cases} 0 & (|r| - \varepsilon \leq 0), \\ |r| - \varepsilon & \text{otherwise,} \end{cases} \quad (12)$$

where r is a residual and α and α_i^* are obtained by solving the following optimization problem:

$$\begin{aligned} \min Q(\alpha, \alpha^*) = & \frac{1}{2} \sum_{i,j=1}^m (\alpha_i - \alpha_i^*)(\alpha_j - \alpha_j^*) K(x_i, x_j) \\ & + \varepsilon \sum_{i=1}^m (\alpha_i + \alpha_i^*) - \sum_{i=1}^m y_i (\alpha_i - \alpha_i^*) \end{aligned} \quad (13)$$

$$\text{s.t.} \quad \begin{cases} \sum_{i=1}^m (\alpha_i - \alpha_i^*) = 0, \\ 0 \leq \alpha_i \leq C, 0 \leq \alpha_i^* \end{cases} \quad (14)$$

5. Results

5.1. Time-series Prediction

The conventional evaluation technique for parameter setting of classification algorithms is based on only the success rate of the classification. In this paper, we use a time-series prediction for evaluation of parameter settings. We performed time-series prediction using three algorithms: ELM, SVR, and back propagation (BP) [8]. Table 3 shows the parameter values used for each algorithm. The parameter values in Table 3 were obtained by trials and errors for each models. Table 4 shows the root-mean-squared error (RMSE) and computation time for the training. Figures 3–5 show the prediction results. ELM has the best performance among the three algorithms for NIRS data prediction, and the best number of hidden-layer neurons for ELM is 27.

5.2. Classification

We used ELM and SVM for classification algorithms. Evaluation of classification ability was performed using 5-fold cross-validation. Table 5 shows parameter values used in each algorithm. Table 6 shows the classification results and computation time for the training.

In the results, the classification rate for ELM was 85.88% and the computation time was 0.023 s. Using SVM, the classification rate was 85.48% and the computation time was 1.487 s. Table 4 thus indicates that ELM performs better than SVM.

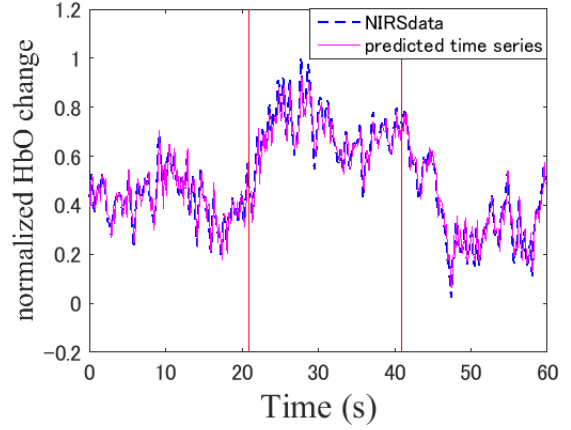


Figure 3: NIRS data (solid line) and predicted time series (dashed line) by ELM.

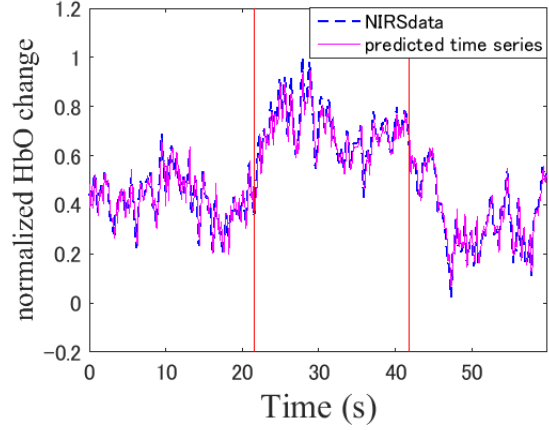


Figure 4: NIRS data (solid line) and predicted time series (dashed line) by BP.

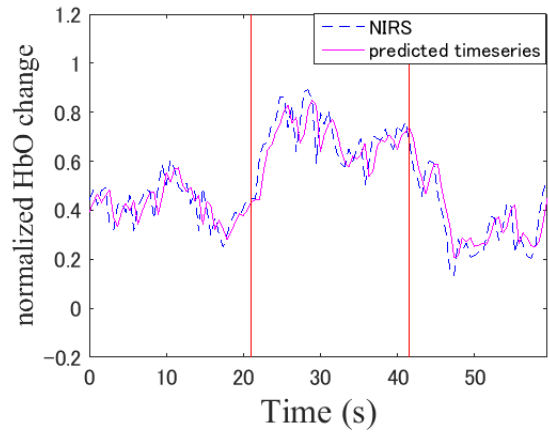


Figure 5: NIRS data (solid line) and predicted time series (dashed line) by SVR.

Table 3: Parameter values used in the three prediction techniques.

	ELM	BP	SVR
Input dimension	9	6	9
Lag	1	1	1
# of training data	1846	1846	461
# of Hidden layer neuron	27	10	(N.A.)
Margin parameter: C	(N.A.)	(N.A.)	26000
width of ε tube: ε	(N.A.)	(N.A.)	9×10^{-7}

Table 4: RMSE and computation time for predictions.

Algorithm	RMSE	Computation time (s)
ELM	0.0425	0.35
BP	0.0435	232.71
SVR	0.0833	11651.22

6. Conclusion

We introduced ELM for time-series prediction and classification of NIRS data. In the results for time-series prediction, we found that ELM is highly suitable for prediction. The results for classification too indicated that ELM has better performance than conventional SVM. We have thus shown that the ELM is an efficient classifier for NIRS data.

In future research we will verify the classification rate with more participants to see whether the proposed classifier is efficient with NIRS signals for other tasks.

Acknowledgments

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Table 5: Parameter values used in the two classifiers.

	ELM	SVM
Input dimension	9	9
Lag	1	1
# of training data	1846	1846
# of Hidden layer neuron	27	(N.A.)
Margin parameter: C	(N.A.)	300
kernel function	(N.A.)	RBF

Table 6: Classification rates and computation times.

Algorithm	Classification rate	Computation time (s)
ELM	85.88	0.02328
SVM	85.48	1.487

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