# SCATTERING OF ELECTROMAGNETIC WAVES BY INHOMOGENEOUS DIELECTRIC GRATINGS WITH PERFECTLY CONDUCTING STRIP 

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## 1. Introduction

Recently, the refractive index can easily be controlled to make the periodic structures such as optoelectronic devices, photonic bandgap crystals, frequency selective devices, and other applications by the development of manufacturing technology of optical devices ${ }^{[1]}$. Thus, the scattering and guiding problems of the inhomogeneous gratings have been considerable interest, and many analytical and numerical methods which are applicable to the dielectric gratings having an arbitrarily periodic structures combination of dielectric and metallic materials ${ }^{[2]}$.

In this paper, we proposed a new method for the scattering of electromagnetic waves by inhomogeneous dielectric gratings with perfectly conducting strip using the combination of improved Fourier series expansion method ${ }^{[3]}$ and point matching method ${ }^{[4]}$. This method also can be applied to the dielectric gratings having an arbitrarily periodic structures combination of dielectric and metallic materials.

## 2. Method of Analysis

We consider inhomogeneous dielectric gratings with perfectly conducting strip as shown in Fig.1(a). The grating is uniform in the $y$-direction and the permittivity $\varepsilon(x, z)$ with respect to the position(=w) is an arbitrary periodic function of $z$ with period $p$. The permeability is assumed to be $\mu_{0}$. The time dependence is $\exp (-i \omega t)$ and suppressed throughout. In the formulation, the TM wave is discussed. When the TM wave (the magnetic field has only the $y$-component) is assumed to be incident from $x>0$ at the angle $\theta_{0}$, the magnetic fields in the regions $S_{1}(x \geq 0)$ and $S_{3}(x \leq-d)$ are expressed ${ }^{[3]}$ as


Fig. 1 Structure of inhomogeneous dielectric grating with perfectly conducting strip.
(a) Coordinate system, (b) Approximated inhomogeneous layers.
$\underline{S_{1}(x \geq 0):} \quad H_{y}^{(1)}=e^{i k_{1}\left(z \sin \theta_{0}-x \cos \theta_{0}\right)}+e^{i k_{1} z \sin \theta_{0}} \sum_{n=-N}^{N} r_{n}^{(1)} e^{i\left(k_{n}^{(1)} x+2 \pi n z / p\right)} ; k_{1} \triangleq \omega \sqrt{\varepsilon_{1} \mu_{0}}$
$\underline{S_{3}(x \leq-d)}: \quad H_{y}^{(3)}=e^{i k_{1} z \sin \theta_{0}} \sum_{n=-N}^{N} t_{n}^{(3)} e^{-i\left\{k_{n}^{(3)}(x+d)-2 \pi n z / p\right\}}$
$k_{n}^{(j)} \triangleq \sqrt{k_{0}^{2} \varepsilon_{j} / \varepsilon_{0}-\gamma_{n}^{2}} ; \gamma_{n} \triangleq k_{1} \sin \theta_{0}+2 \pi n / p, k_{0} \triangleq 2 \pi / \lambda, j=1,3$.
where $\lambda$ is the wavelength in free space, $r_{n}^{(1)}$, and $t_{n}^{(3)}$ are unknown coefficients to be determined by boundary conditions.
Main process of our method to treat these problems is as follows (see Fig.1(b)):
(1) First, the grating layer $(-d<x<0)$ is approximated by an assembly of $M$ stratified layers of modulated index profile with step size $d_{\Delta}(\triangleq d / M)$ approximated to step index profile $\varepsilon^{(l)}(z)\left[\triangleq \varepsilon\left((l+0.5) d_{\Delta}, z\right) ; \quad l=1 \sim M\right]$, and the magnetic fields are expanded appropriately by a finite Fourier series.

$$
\begin{equation*}
\underline{S_{2}(-d<x<0)}: H_{y}^{(l, 2)}=\sum_{v=1}^{2 N+1}\left[A_{v}^{(l)} e^{i h_{v}^{(l)}\left\{x+(l-1) d_{\Delta}\right\}}+B_{v}^{(l)} e^{i h_{v}^{(l)}\left(x+l d_{\Delta}\right)}\right] e^{i k_{1} z \sin \theta_{0}} \sum_{n=-N}^{N} u_{v, n}^{(l)} e^{i 2 \pi n z / p} \tag{3}
\end{equation*}
$$

where $h_{v}^{(l)}$ is the propagation constant in the $x$-direction.
We get the following eigenvalue equation in regard to $h^{(l)[3]}$

$$
\begin{equation*}
\Lambda_{1} \mathbf{U}^{(l)}=\left\{h^{(l)}\right\}^{2} \Lambda_{2} \mathbf{U}^{(l)} ; \Lambda_{1} \triangleq\left[\eta_{m, n}^{(l)}\right], \Lambda_{2} \triangleq\left[\zeta_{m, n}^{(l)}\right], l=1 \sim M \tag{4}
\end{equation*}
$$

where,

$$
\begin{align*}
& \mathbf{U}^{(l)} \triangleq\left[u_{-N}^{(l)}, \cdots, u_{0}^{(l)}, \cdots u_{N}^{(l)}\right]^{T}, T: \text { transpose } \\
& \zeta_{n, m}^{(l)} \triangleq k_{0}^{2} \xi_{n, m}^{(l)}-\gamma_{n}\left\{\gamma_{n} \eta_{n, m}^{(l)}+2 \pi(n-m) \eta_{n, m}^{(l)} / p\right\}, \quad \gamma_{n}^{(l)} \triangleq\left(k_{1} \sin \theta_{0}+2 \pi n / p\right),  \tag{5}\\
& \eta_{n, m}^{(l)} \triangleq \frac{1}{p} \int_{0}^{p}\left\{\varepsilon^{(l)}(z)\right\} e^{i 2 \pi(n-m) z / p} d z, \xi_{n, m}^{(l)} \triangleq \frac{1}{p} \int_{0}^{p}\left\{\varepsilon^{(l)}(z)\right\}^{2} e^{i 2 \pi(n-m) z / p} d z, m, n=-N, \cdots, 0, \cdots N .
\end{align*}
$$

For the TM case, the permittivity profile approximated by a Fourier series of $N_{f}$ terms ${ }^{[3]}$ and $N_{f}$ is related to the modal truncation number $N\left(N=1.5 N_{f}\right){ }^{[3]}$.
(2) Second, the strip region $(j<l<j+1)$, see Fig.1(b), we obtain the matrix form combination of metallic region $C$ and the dielectric region $\bar{C}$ using boundary condition at the matching points $z_{k}(=p k /(2 N+1), k=0, \cdots 2 \mathrm{~N})$ on $x=-l \cdot d_{\Delta}(l=j)$.Boundary condition are as follows:
$z_{k} \in C:\left[E_{z}^{(2, j)}=E_{z}^{(2, j+1)}=0\right]$
$\sum_{v=1}^{2 N+1} h_{v}{ }^{(j)}\left[A_{v}^{(j)} e^{i h_{v}^{(j)} d_{\Delta}}-B_{v}^{(j)}\right] \cdot \sum_{n=-N}^{N} u_{n, v}^{(j)} e^{i n z_{k}}=0, \sum_{v=1}^{2 N+1} h_{v}^{(j+1)}\left[A_{v}^{(j+1)}+B_{v}^{(j+1)} e^{i h_{v}(j+1)} d_{\Delta}\right] \cdot \sum_{n=-N}^{N} u_{n, v}^{(j+1)} e^{i n z_{k}}=0$
$z_{k} \in \bar{C}:\left[H_{y}^{(2, l)}=H_{y}^{(2, l+1)}\right]$
$\sum_{v=1}^{2 N+1}\left[A_{v}^{(j)} e^{i h_{v}^{(j)} d_{\Delta}}+B_{v}^{(j)}\right] \cdot \sum_{n=-N}^{N} u_{n, v}^{(j)} e^{i n z_{k}}=\sum_{v=1}^{2 N+1}\left[A_{v}^{(j+1)}+B_{v}^{(j+1)} e^{i h_{v}^{(j+1)} d_{\Delta}}\right] \cdot \sum_{n=-N}^{N} u_{n, v}^{(j+1)} e^{i n z_{k}}$
$z_{k} \in \bar{c}\left[E_{z}^{(2, j)}=E_{z}^{(2, j+1)}\right]: \quad \frac{1}{\varepsilon^{(j)}(z)} \sum_{v=1}^{2 N+1} h_{v}^{(j)}\left[A_{v}^{(j)} e^{i h_{v}^{(j)} d_{\Delta}}-B_{v}^{(j)}\right] \cdot \sum_{n=-N}^{N} u_{n, v}^{(j)} e^{i n z_{k}}=$

$$
\begin{equation*}
\frac{1}{\varepsilon^{(j+1)}(z)} \sum_{v=1}^{2 N+1} h_{v}^{(j+1)}\left[A_{v}^{(j+1)}+B_{v}^{(j+1)} e^{i h_{v}^{(j+1)} d_{\Delta}}\right] \cdot \sum_{n=-N}^{N} u_{n, v}^{(j+1)} e^{i n z_{k}} \tag{8}
\end{equation*}
$$

In the Eq.(8), the boundary condition at $E_{z}^{(2, j)}=E_{z}^{(2, j+1)}$, it is satisfied in all matching points. Therefor, rearranging after multiplying both sides $\varepsilon_{j}(z) \cdot \varepsilon_{j+1}(z)$ in Eq.(8) by using the orthogonality properties of $\left\{e^{i 2 \pi n z / p}\right\}$, we get following equation.

$$
\begin{equation*}
\sum_{v=1}^{2 N+1} h_{V}^{(j)}\left[A_{V}^{(j)} e^{i h_{V}^{(j)} d_{\Delta}}-B_{V}^{(j)}\right] \cdot \phi_{n, v}^{(j)}=\sum_{v=1}^{2 N+1} h_{v}^{(j+1)}\left[A_{V}^{(j+1)}-B_{V}^{(j+1)} e^{i h_{v}^{(j+1)} d_{\Delta}}\right] \cdot \psi_{n, v}^{(j+1)} \tag{9}
\end{equation*}
$$

where

$$
\phi_{n, v}^{(j)} \triangleq \sum_{m=-N}^{N} u_{v, m}^{(j)} \eta_{m, n}^{(j+1)}, \quad \psi_{n, v}^{(j+1)} \triangleq \sum_{m=-N}^{N} u_{v, m}^{(j+1)} \eta_{m, n}^{(j)}, \quad n=-N, \cdot \cdot, 0, \cdot \cdot N
$$

By using matrix algebra in Eq.(9), we get following matrix form.
$\Phi^{(j)} \mathbf{C}^{(j)}\left[\mathbf{D}^{(j)} \mathbf{A}^{(j)}-\mathbf{B}^{(j)}\right]=\Psi^{(j+1)} \mathbf{C}^{(j+1)}\left[\mathbf{A}^{(j+1)}-\mathbf{D}^{(j+1)} \mathbf{B}^{(j+1)}\right]$,
$\left[\mathbf{D}^{(j)} \mathbf{A}^{(j)}-\mathbf{B}^{(j)}\right]=\left[\Phi^{(j)} \mathbf{C}^{(j)}\right]^{-1} \cdot\left[\Psi^{(j+1)} \mathbf{C}^{(j+1)}\right]\left[\mathbf{A}^{(j+1)}-\mathbf{D}^{(j+1)} \mathbf{B}^{(j+1)}\right]=\boldsymbol{\Theta}\left[\mathbf{A}^{(j+1)}-\mathbf{D}^{(j+1)} \mathbf{B}^{(j+1)}\right]$,
where
$\Phi^{(j)} \triangleq\left[\phi_{n, v}^{(j)}\right], \Psi^{(j+1)} \triangleq\left[\psi_{n, v}^{(j+1)}\right], \mathbf{C}^{(j)} \triangleq\left[h_{v}^{(j)} \cdot \delta_{(n+N+1), v}\right], \mathbf{D}^{(j)} \triangleq\left[e^{i h_{\nu}^{(j)} d_{\Delta}} \cdot \delta_{(n+N+1), v}\right]$,
$\Theta \triangleq\left[\theta_{n, v}^{(j, j+1)}\right]=\left[\Phi^{(j)} \mathbf{C}^{(j)}\right]^{-1} \cdot\left[\Psi^{(j+1)} \mathbf{C}^{(j+1)}\right], \delta_{(n+N+1), v} ;$ Kronecker's delta.

We get following matrix form combined with Eq.(6) and Eq.(7).

$$
\begin{align*}
& \mathbf{H}^{\prime(j)}\left[\mathbf{D}^{(j)} \mathbf{A}^{(j)}+\mathbf{D}^{(j)} \mathbf{B}^{(j)}\right]=\mathbf{H}^{\prime(j+1)}\left[\mathbf{A}^{(j+1)}+\mathbf{D}^{\prime(j+1)} \mathbf{B}^{(j+1)}\right]  \tag{11}\\
& \mathbf{V}_{1}{ }^{(j)} \mathbf{A}^{(j)}+\mathbf{V}_{2}{ }^{(j)} \mathbf{B}^{(j)}=\mathbf{V}_{3} \mathbf{A}^{(j+1)}+\mathbf{V}_{4} \mathbf{B}^{(j+1)} \tag{12}
\end{align*}
$$

where
$\left.\mathbf{H}^{\prime(j)}=\left[\begin{array}{cccccc}\vdots & \vdots & \vdots & & \vdots & \vdots \\ e^{-i N z k} & \cdots & e^{i 0 z k} & \cdots & e^{i N z k} \\ \vdots & \vdots & \vdots & & \vdots & \vdots \\ e^{-i N z k} & \cdots & e^{i 0 z k} & \cdots & e^{i N \Sigma k}\end{array}\right]\right\} z_{k} \in c \cdot \mathbf{U}^{(j)}$,

$$
\left[\begin{array}{l}
\mathbf{D}^{{ }^{(j)} \triangleq} \triangleq\left[\eta e^{i h_{v}^{(j)} d_{\Delta}} \cdot \delta_{(n+N+1), v}\right], \\
\eta=h_{v}^{(j)} ; z_{k} \in c, \quad \eta=1 ; z_{k} \in \bar{c} \\
\mathbf{D}^{\prime(j) \triangleq} \triangleq\left[\eta \cdot \delta_{(n+N+1), v}\right] \\
\eta=-h_{v}^{(j)} ; z_{k} \in c, \eta=1 ; z_{k} \in \bar{c}
\end{array}\right.
$$

$\left.\mathbf{H}^{(j+1)}=\left[\begin{array}{ccccc}\vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & \cdots & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ e^{-i N z k} & \cdots & e^{i 0 z k} & \cdots & e^{i N z k}\end{array}\right]\right\} \begin{gathered} \\ z_{k} \in c \\ \\ \\ z_{k} \in \bar{c}\end{gathered}$
$\mathbf{D}^{\prime(j+1)} \triangleq\left[e^{i h_{l}^{(j+1)} d_{\Delta}} \cdot \delta_{(n+N+1), v}\right]$
$\mathbf{V}_{1} \triangleq\left[v_{n, v}^{(1)}\right]=\left[\mathrm{H}^{\prime^{(j)}} \mathrm{D}^{(j)}\right] \quad, \quad \mathbf{V}_{2} \triangleq\left[v_{n, v}^{(2)}\right]=\left[\mathrm{H}^{(j)} \mathrm{D}^{(j)}\right] \quad, \quad \mathbf{V}_{3} \triangleq\left[v_{n, v}^{(3)}\right]=\mathrm{H}^{(j+1)} \quad$,
$\mathbf{V}_{4} \triangleq\left[v_{n, v}^{(4)}\right]=\left[\mathrm{H}^{\prime(j+1)} \mathrm{D}^{\prime(j+1)}\right]$
By using matrix algebra in Eq.(10) and (12), we get following matrix relationship between $\mathbf{A}^{(1)}, \mathbf{B}^{(1)}$ and $\mathbf{A}^{(M)}, \mathbf{B}^{(M)}$.
$\binom{\mathbf{A}^{(j)}}{\mathbf{B}^{(j)}} \triangleq\left(\begin{array}{ll}\mathbf{S}_{1}^{(j)} & \mathbf{S}_{2}^{(j)} \\ \mathbf{S}_{3}^{(j)} & \mathbf{S}_{4}^{(j)}\end{array}\right)\binom{\mathbf{A}^{(j+1)}}{\mathbf{B}^{(J+1)}}$,
where
$\mathbf{S}_{k}^{(j)} \triangleq\left[{ }^{(j)} s_{n, v}^{(k)}\right], \quad k=1 \sim 4$,
${ }^{(j)} s_{n, v}^{(1)} \triangleq\left[\mathbf{V}_{1}+\mathbf{V}_{2} \cdot \mathbf{D}^{(j)}\right]^{-1} \cdot\left[\mathbf{V}_{3}+\mathbf{V}_{2} \cdot \boldsymbol{\theta}\right]$,
${ }^{(j)} s_{n, v}^{(2)} \triangleq\left[\mathbf{V}_{1}+\mathbf{V}_{2} \cdot \mathbf{D}^{(j)}\right]^{-1} \cdot\left[\mathbf{V}_{4}-\mathbf{V}_{2} \cdot \boldsymbol{\theta} \cdot \mathbf{D}^{(j+1)}\right], \quad{ }^{(j)} s_{n, v}^{(3)} \triangleq\left[{ }^{(j)} s_{n, v}^{(1)}\right] \cdot \mathbf{D}^{(j)}-\boldsymbol{\theta}$,
${ }^{(j)} s_{n, v}^{(4)} \triangleq\left[{ }^{(j)} s_{n, v}^{(2)}\right] \cdot \mathbf{D}^{(j)}+\boldsymbol{\theta} \cdot \mathbf{D}^{(j+1)}$.
(3) Finally, we obtain the relationship between $\mathbf{A}^{(1)}, \mathbf{B}^{(1)}$ and $\mathbf{A}^{(M)}, \mathbf{B}^{(M)}$ using boundary condition at $x=-l \cdot d_{\Delta}(l=1 \sim M-1)$.

$$
\binom{\mathbf{A}^{(1)}}{\mathbf{B}^{(1)}} \triangleq\left(\begin{array}{ll}
\mathbf{S}_{1}^{(1)} & \mathbf{S}_{2}^{(1)}  \tag{14}\\
\mathbf{S}_{3}^{(1)} & \mathbf{S}_{4}^{(1)}
\end{array}\right) \cdot\left(\begin{array}{ll}
\mathbf{S}_{1}^{(2)} & \mathbf{S}_{2}^{(2)} \\
\mathbf{S}_{3}^{(2)} & \mathbf{S}_{4}^{(2)}
\end{array}\right) \ldots\left(\begin{array}{ll}
\mathbf{S}_{1}^{(j)} & \mathbf{S}_{2}^{(j)} \\
\mathbf{S}_{3}^{(j)} & \mathbf{S}_{4}^{(j)}
\end{array}\right) \cdots\left(\begin{array}{ll}
\mathbf{S}_{1}^{(M)} & \mathbf{S}_{2}^{(M)} \\
\mathbf{S}_{3}^{(M)} & \mathbf{S}_{4}^{(M)}
\end{array}\right)\binom{\mathbf{A}^{(M)}}{\mathbf{B}^{(M)}}=\left(\begin{array}{ll}
\mathbf{S}_{1} & \mathbf{S}_{2} \\
\mathbf{S}_{3} & \mathbf{S}_{4}
\end{array}\right)\binom{\mathbf{A}^{(M)}}{\mathbf{B}^{(M)}}
$$

where $l \neq j \quad \mathbf{S}_{k}^{(l)} \triangleq\left[{ }^{(l)} S_{n, v}^{(k)}\right], \quad k=1 \sim 4, l=1 \sim M$,

$$
\begin{array}{ll}
{ }^{(l)} s_{n, v}^{(1)} \triangleq \frac{1}{2}\left[v_{n, v}^{(l)}+\theta_{n, v}^{(l)} h_{n+N+1}^{(l+1)} / h_{v}^{(l)}\right] e^{-i h_{v}^{(l)} d_{\Delta}}, & { }^{(l)} s_{n, v}^{(2)} \triangleq{ }^{(l)} S_{n, v}^{(3)} \cdot e^{i\left\{h_{n+N+1}^{(l+1)}-h_{v}^{(l)}\right\} d_{\Delta}}, \\
{ }^{(l)} s_{n, v}^{(3)} \triangleq \frac{1}{2}\left[v_{n, v}^{(l)}-\theta_{n, v}^{(l)} h_{n+N+1}^{(l+1)} / h_{v}^{(l)}\right], & { }^{(l)} s_{n, v}^{(4)} \triangleq \frac{1}{2}\left[v_{n, v}^{(l)}+\theta_{n, v}^{(l)} h_{n+N+1}^{(l+1)} / h_{v}^{(l)}\right] e^{i h_{n+N+1}^{(1)} d_{\Delta}}, \\
\mathbf{V} \triangleq\left[\mathbf{v}_{n, v}^{(l)}\right]=\left[\mathbf{U}^{(l)}\right]^{-1} \cdot\left[\mathbf{U}^{(l+1)}\right], & \Theta \triangleq\left[\theta_{n, v}^{(l)}\right]=\left[\Phi^{(l)}\right]^{-1} \cdot\left[\Psi^{(l+1)}\right] .
\end{array}
$$

Using Eq.(14), we get the following homogeneous matrix equation in regard to $A^{(M)}$.

$$
\begin{aligned}
& \mathbf{W} \cdot \mathbf{A}^{(M)}=\mathbf{F}, \quad \mathbf{W} \triangleq\left[\mathbf{Q}_{1} \mathbf{S}_{1}+\mathbf{Q}_{2} \mathbf{S}_{3}-\left(\mathbf{Q}_{1} \mathbf{S}_{2}+\mathbf{Q}_{2} \mathbf{S}_{4}\right) \mathbf{Q}_{4}^{-1} \mathbf{Q}_{3}\right], \\
& \text { where }, \mathbf{F} \triangleq\left[2 k_{0}^{(1)} \eta_{0,-N}^{(1)}, \cdots, 2 k_{0}^{(1)} \eta_{0,0}^{(1)}, \cdots, 2 k_{0}^{(1)} \eta_{0, N}^{(1)}\right]^{T} \\
& \quad \mathbf{Q}_{k} \triangleq\left[q_{v, n}^{(k)}\right] ; k=1 \sim 4, \\
& q_{v, n}^{(1)} \triangleq\left[h_{v}^{(1)} u_{v, n}^{(1)}+\sigma_{v, n}^{(1)}\right], \quad q_{v, n}^{(2)} \triangleq-\left[h_{v}^{(1)} u_{v, n}^{(1)}-\sigma_{v, n}^{(1)}\right] e^{i h_{v}^{(1)} d_{\Delta}} \\
& q_{v, n}^{(3)} \triangleq\left[h_{v}^{(M)} u_{v, n}^{(M)}-\sigma_{v, n}^{(M)}\right] e^{i h_{v}^{(M)} d_{\Delta}}, \quad q_{v, n}^{(4)} \triangleq-\left[h_{v}^{(M)} u_{v, n}^{(M)}+\sigma_{v, n}^{(M)}\right] \\
& \sigma_{v, n}^{(1)} \triangleq \sum_{m=-N}^{N} \varepsilon_{0} k_{m}^{(1)} u_{v, n}^{(1)} \eta_{m, n}^{(1)} / \varepsilon_{1}, \quad \sigma_{v, n}^{(M)} \triangleq \sum_{m=-N}^{N} \varepsilon_{0} k_{m}^{(3)} u_{v, n}^{(M)} \eta_{m, n}^{(M)} / \varepsilon_{3} \\
& n=-N, \cdots, 0, \cdots, N, \quad v=1 \sim(2 N+1)
\end{aligned}
$$

The mode power transmission coefficients $\left|T_{n}^{(T M)}\right|^{2}$ is given by

$$
\begin{equation*}
\left|T_{n}^{(T M)}\right|^{2} \triangleq \varepsilon_{1} \operatorname{Re}\left\{k_{n}^{(3)}\right\}\left|t_{n}^{(3)}\right|^{2} /\left(\varepsilon_{3} k_{0}^{(1)}\right) \tag{16}
\end{equation*}
$$

where superscript (TM) indicates TM wave case.

## 3. Conclusion

In this paper, we have proposed a new method for the scattering of electromagnetic waves by inhomogeneous dielectric gratings with perfectly conducting strip using the combination of improved Fourier series expansion method and point matching method. This method can be applied to the dielectric gratings having an arbitrarily periodic structures combination of dielectric and metallic materials.

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