Designed of a Broadband Multi-Layered Absorber using an NSGA-II Multi-Objective Optimization Algorithm

Ki-Bum Jung, Hyun-Su Shin, Yeon-Choon Chung, and Jae-Hoon Choi

Senior Member of Technical Staff /P.L, EMC Center 901, Hogye-2dong, Dongan-gu, Anyang-si, Kyunggi-do, 430-082, Korea E-mail: kbjung@rapa.or.kr

School of Engineering, div . Of Electrical and Computer, Hanyang University 17 Haengdang-dongs, Seongdong-gu, Seoul, 133-791, Korea

E-mail: <u>hssshinhyu@ihanyang.ac.kr</u>

Department of Information and Communication Engineering, Seokyeong University 16-1 Jungneung-Dong Sungbuk-Ku Seoul, 136-704 Korea

E-mail: <u>ycchung@skuniv.ac.kr</u>

Div . Of Electrical and Computer, Hanyang University 17 Haengdang-dongs, Seongdong-gu, Seoul, 133-791, Korea

E-mail: choijh@hanyang.ac.kr

Abstract: In this paper, we purpose multi-objective optimization genetic algorithm implementation for optimum design of slim multilayer absorber. Among multi-objective optimization technique, applied by first in NSGA-II(Non-dominated Sorting Genetic Algorithm) genetic algorithm slim multilayer absorber field that is attested that performance is excellent. Slim multilayer absorber composes insulator in incidence angle within 30 angle and limited extent by number of layers within total 5 layers including top floor. Numerical analysis algorithm embodied optimization algorithm to use material information collected actually considering manufacture. Here after, is going to compare and examine measurement through manufacture and numerical analysis result.

1. Introduction

In this paper, multi-objective evolutionary algorithms(MOEA) are used to optimize the structure of electromagnetic wave absorbers. optimization problems involve multiple conflicting objectives, such as simultaneous minimization of production cost and maximization of durability. Under this conflicting situation, it is intuitive that less costly objective is usually less durable and vice versa, therefore multi-objective optimization technique has to be adapted and slim multilayer absorbers are to be optimized by using NSGA-II which is able to find much better spread of solution and better convergence near the true pareto-optimal front compared to any other MOEAs. Given a predefined set of available-existent and virtual-materials with frequency-dependent permittivity and permeability, the proposed technique simultaneously determines the optimal material choice for each layer, its thickness, and fractional bandwidth. This optimal choice results in more excellent multilayer absorbers, which maximally absorbers TE and TM incident

plane waves for the prescribed range of frequencies and incident angle, than those of previous studies.

2. Reflection Coefficient of a Slim Multi-Layer Absorber Medium

The Propagation wave of a flat multi-layered isotropic medium is described by a scalar wave equation in TE and TM respectively. Such a two scalar wave equations are described very simple with think of one dimensional problem. To begin with, accepted field from source excitation in flat multi-layer type medium can be expression a form of an integral equation. This is represented better of the simple equation through asymptotic expansion method.

2.1 Induced of Scalar Wave Equations

We have induced in this case TE and TM. On the basis of orthogonal coordinates, propagation of direction z-axis suppose to TE wave. In this case electrical field must be presence x-y plane. If considering to arbitrary y-axis direction element, then electrical field is presented at E=Ey.

$$\mu \nabla \times \mu^{-1} \nabla \times E_{y} - \omega^{2} \mu \varepsilon E_{y} = 0 \tag{1}$$

Here, if $\partial/\partial y E_y = 0$ is concluded, therefore next some condition is achieved.

$$\nabla \cdot \varepsilon E_{y} = \frac{\partial}{\partial y} \varepsilon(z) E_{y} = 0 \tag{2}$$

If arrange y-axis direction element, equation forms as following.

$$\left[\frac{\partial^2}{\partial x^2} + \mu(z)\frac{\partial}{\partial y}\mu^{-1}(z)\frac{\partial}{\partial z} + \omega^2\mu\varepsilon\right]E_y = 0$$
 (3)

Magnetic field equation about TE wave can derive applying condition ($E_z = 0$, $H_z \neq 0$) about TE wave. The following is vector wave equation about magnetic field in inhomogeneous medium.

$$\varepsilon \nabla \times \varepsilon^{-1} \nabla \times H_z - \omega^2 \mu \varepsilon H_z = 0 \tag{4}$$

And if permittivity and permeability say that is variable z function, can arrange as following.

$$\left[\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \mu(z) \frac{\partial}{\partial z} \mu^{-1}(z) \frac{\partial}{\partial z} + \omega^2 \mu \varepsilon \right] \mu H_z = 0$$
(6)

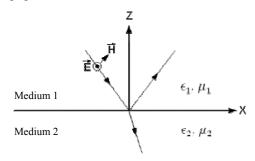
We can be derived boundary condition of scalar wave equation if basic boundary condition $\hat{n} \times E$, $\hat{n} \times H$ is continuity in two medium. The following is boundary condition of electric field and magnetic field about y component in border between medium 1 and medium 2.

$$e_y$$
; $e_{1y} = e_{2y}$, $\mu_1^{-1} \frac{d}{dz} e_{1y} = \mu_2^{-1} \frac{d}{dz} e_{2y}$ (9-a)

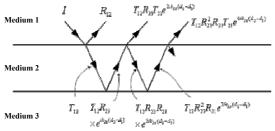
$$h_y$$
: $h_{1y} = h_{2y}$, $\varepsilon_1^{-1} \frac{d}{dz} h_{1y} = \varepsilon_2^{-1} \frac{d}{dz} h_{2y}$ (9-b)

2.2 Reflection coefficient in Half-Space

We suppose that TE wave with below Fig. 1 propagation in different two mediums.



(a) Transmission and reflection coefficient between medium.



(b) Multiple reflection in 3 layers medium

Fig. 1. Multiple reflection principle in between medium

Reflection coefficient and transmission coefficient in two medium is as following if express y-component electric field.

$$e_{1v}(z) = e_0 e^{-ik_{1z}z} + R^{TE} e_0 e^{ik_{1z}z}$$
 (10)

$$e_{2v}(z) = T^{TE}e_0e^{-ik_{2z}z}$$
 (11)

Eq. (10) expresses electric field by linear reiteration principle of $\exp(\pm i k_{1z} z)$ from upper part half space, and eq. (11) expresses electric field from below part half space. Here, R^{TE} and T^{TE} mean TE wave reflection coefficient and transmission coefficient each. Subscript 1y, 2y, 1z, and 2z mean medium and direction. Therefore, reflection coefficient and transmission coefficient of transverse electric wave can express as following.

$$R^{TE} = \frac{-\mu_{1}k_{2z} + \mu_{2}k_{1z}}{\mu_{1}k_{2z} + \mu_{2}k_{1z}}, R^{TM} = \frac{-\varepsilon_{1}k_{2z} + \varepsilon_{2}k_{1z}}{\varepsilon_{1}k_{2z} + \varepsilon_{2}k_{1z}}$$

$$(12-a)$$

$$T^{TE} = \frac{2\mu_{2}k_{1z}}{\mu_{1}k_{2z} + \mu_{2}k_{1z}}, T^{TM} = \frac{2\varepsilon_{2}k_{1z}}{\varepsilon_{1}k_{2z} + \varepsilon_{2}k_{1z}}$$

$$(12-b)$$

We can become expressed briefly as follows if generalize little more eq. (12).

$$\overline{R}_{i,i+1} = \frac{R_{i,i+1} + \overline{R}_{i+1,i+2} e^{2ik_{i+1,z}(d_{i+1} - d_i)}}{1 - R_{i+1,i}\overline{R}_{i+1,i+2} e^{2ik_{i+1,z}(d_{i+1} - d_i)}}$$
(13)

Finally, we can save reflection coefficient of multilayer medium applying circulation expression with eq. (13) if find out frequency, properties of matter (permittivity, permeability), thickness of medium. We can puts air on first layer and puts PEC on last layer and saves reflection coefficient if apply to multi-layer absorber material of this study.

3. Multi-objective optimization genetic algorithm

Genetic algorithm is algorithm that based on choice of natural world and mechanism of genetics. Usually, evolution algorithm can divide by genetic algorithm and evolution strategy. Optimization searching process of genetic algorithm is consisted of greatly subsequent 4 steps. The first is initialization, and second fitness estimation, third reproduction (use of heredity operator), fourth by END condition examination and loop consist. Since VEGA that multi-objective most suitable algorithm is first gene algorithm for multi-objective problem by Schaffer in 1988 is announced, there were a lot of developments until present. In this paper, embodied multi-objective algorithm of pareto base in optimum design of multi-layer absorber. But, multi-objective algorithm

complexity of calculation is big, and does not use elit strategy, and have uncomfortable though set share parameter. To supplement this weak point, K. Deb proposed multi-objective evolutionary algorithm of non-dominated sorting. We that apply this evolutionary algorithm completed numerical analysis algorithm of slim multi-layer absorber structure.

Table 1. Fast non-dominated sorting procedure

fast-non-dominated sort (P)				
for each $p \in F$				
$S_p = \emptyset$				
$n_p = 0$				
for each $q \in F$				
if $(p < q)$ then	If p dominates q			
$S_p = S_p \cup \{q\}$	Add q to the set of solutions dominated by p			
else if $(q < p)$ the				
$n_p = n_p + 1$	Increment the domination counter of p			
if $n_p = 0$ then	p belongs to the first front			
$p_{rank} = :$				
$F_1 = F_1 \cup \{p\}$				
i = 1	Initialize the front counter			
while $F_i \neq \emptyset$				
$Q = \emptyset$	Used to store the members of the next front			
for each $p \in F$				
for each $q \in S_{k}$				
$n_{\sigma} = n_{\sigma} - 1$				
if $n_q = 0$ then	q belongs to the next front			
$q_{rank} = i +$				
$Q = Q \cup \{q$				
i = i + 1				
$F_i = \zeta$				

Table 2. Optimization algorithm main loop that elitism is applied

Main Loop (elitism)				
$R_i = P_i \cup C_i$				
	- combine parent and offspring population			
$F = \text{fast-non-dominated-sort}(R_t)$				
	- $F = (F_1, F_2,)$, all nondominated fronts of R_t			
$P_{i+1} = \emptyset$ and $i = 1$				
until $ P_{i+1} + F_i $	- until the parent population is filled			
crowding-distance-assignment (F_i) - calculate crowding-distance in F_i				
	- include ith nondominated front in the perent pop			
$Sort(F_i, <)$	- sort in descending order using <,			
$P_{i+1} = P_{i+1} \cup F_i$ [1	"			
	- choose the first $(N- P_{i+1} $ elements of F_i			
$Q_{t+1} = \text{make-new}$	* * * * * * * * * * * * * * * * * * *			
-4T1	- use selection, crossover and mutation			
	to create a new population Q_{i+} :			
t = t + 1	- increment the generation counter			

Table 1 shows calculation of O (MN2) that is reduction than calculation of fast nondominated sorting procedure and existing. Elitism applied in this optimization algorithm compares population of present with non-dominated solution of good quality in ago generation. It is Table 2 that explains this.

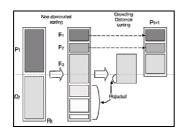


Fig. 2. NSGA-II procedure

Also, this Table 2 and Fig. 2 display NSGA-II's procedure. Three advantages of NSGA-II are fast nondominated sorting procedure, fast crowded distance estimation procedure, and simple crowded comparison operator.

4. Optimum design of slim multilayer absorber

Fig. 3 displays slim multilayer absorber composition. Least significant layer puts metal material. Arrange absorption material that get thin n-1 more from 1 layer. And top-level layer locates insulator.

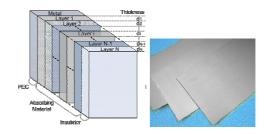
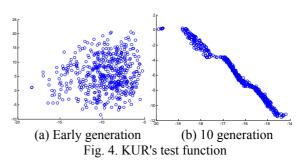


Fig. 3. Structure of slim multilayer absorber

4.1 Numerical analysis result

Estimated accuracy of algorithm that is embodied in this study through test function used in KUR's study.



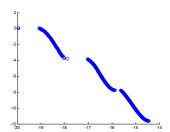


Fig. 5. 50 generation of KUR test function

Expected pareto front of this test function is non-convex's type.

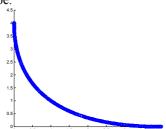


Fig. 6. 50 generation of Schaffer (SCH) test function

In this study, material of kind that displayed material property used total 28.

Table 3. Most suitable design variables that do not consider insulation

Designed Number #53						
Layer Number	Material Number		Thickness(μm)			
1	20		312.06			
2	13		369.45			
3	15		654.21			
4	6		323.47			
Best reflection coefficient in bandwidth		-23.042(TE), -15.1(TM)				
(dB)						
Total Thickness(μm)		1659.2				

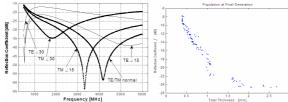


Fig. 7. Reflection coefficient property by incidence angle of designed number #53 absorber.

Table 4. Optimization designed variable of 500 MHz ~ 6 GHz band absorber

Designed Number # 71						
Layer number	Material numb	Thickness(μm)				
1	19		250.45			
2	17		250.05			
3	12		919.86			
4	26		604.94			
5	permittivity (4.0073+j0)		254.21			
Best reflection coefficient in bandwidth (dB)			-9.5697			
Total thickness(µm)		2279.5				

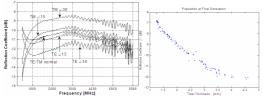


Fig. 8. Reflection coefficient property by incidence angle of design number #71 absorber

5. Conclusion

In this paper, we designed broadband multi-layered absorber using proposed a computationally fast and elitist multi-objective evolutionary algorithm based on non-dominated sorting approach. In most objective functions, NSGA-II has found a better spread of solution than general proposed multi-objective algorithm. We will study a slim multi-layered broadband absorber practice technology to solve EMI problem of PCB level.

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