

TIME DOMAIN WAVE FORM IN ELECTROMAGNETIC
SCATTERING BY A CONDUCTING WEDGE

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In order to find the size of the scatters, it is important to study the time domain wave form in electromagnetic scattering by a conducting wedge. For which a simple model i.e., step function and delta function are selected as a pulse source.

A analytical expression for the electromagnetic scattering by a conducting wedge in steady state as shown in Fig. 1

$$\frac{E_z^S(\rho, \omega)}{E_0(\omega)} = \frac{4\pi}{\Phi_0} \sum_{n=1}^{\infty} J_{\nu_n}\left(\frac{\omega}{c_0}\rho\right) e^{j\frac{\nu_n}{2}\pi} \sin(\nu_n\phi_s) \sin(\nu_n\phi) - e^{j\frac{\omega}{c_0}\rho \cos(\phi_s-\phi)} \quad (1)$$

where $\nu_n = \frac{n\pi}{\Phi_0}$, $\Phi_0 = 2\pi - \Phi_w$

In which the first term gives total field by scattering and second incident field.

To obtain the time domain in electromagnetic field, following Fourier transform is used:

$$E_z^S(\rho, t) = \int_{-\infty}^{\infty} E_z^S(\rho, \omega) e^{j\omega t} d\omega \quad (2)$$

In generally, it is very difficult to perform the above integral. Fortunately the transfer function or integrand including $J_{\nu_n}\left(\frac{\omega}{c_0}\rho\right)$ in expression has a simple form of the integrand, so that it can be easily integrated in this case.

For the numerical example two models are used

(a) Step function

$$U(t) = \begin{cases} 1 & t > 0 \\ 0 & t < 0 \end{cases} \quad (3)$$

For which the time domain in field expression is exactly obtained as

$$E_z^S(t, \rho, \phi, \phi_s) = \frac{2}{e^{j\pi/2\Phi_0}} \sum_{n=1}^{\infty} e^{j\frac{\nu_n}{2}\pi} \sin(\nu_n\phi_s) \sin(\nu_n\phi)$$

$$\left\{ \frac{e^{j\frac{1}{2}v_n\pi} - e^{-j\frac{3}{2}v_n\pi}}{v_n} \right\} \left\{ \frac{\rho/c_0}{t + \sqrt{t^2 - (\rho/c_0)^2}} \right\}^{v_n} - 1 \quad (4)$$

(b) Delta function

For which the field expression is also exactly obtained as

$$E_z^s(t, \rho, \phi, \phi_s) = \frac{2e^{j\pi/2}}{\phi_0 \sqrt{t^2 - (\rho/c_0)^2}} \sum_{n=1}^{\infty} e^{j\frac{v_n}{2}\pi} \sin(v_n\phi_s) \sin(v_n\phi) \cdot \frac{(\rho/c_0)^{v_n} \left\{ e^{j\frac{1}{2}v_n\pi} - e^{-j\frac{3}{2}v_n\pi} \right\}}{\{t + \sqrt{t^2 - (\rho/c_0)^2}\}^{v_n}} - \delta\{\rho/c_0 \cos(\phi_s - \phi) + t\} \quad (5)$$

In Fig. 2(a)(b) the numerical data are shown. This effect for Fig. 2(a) looks like the transient curve for the electrical circuit of L and R. Therefore transient effect for $\phi_w=0$ is largest. No transient phenomenon $\phi_w=180^\circ$ observes.

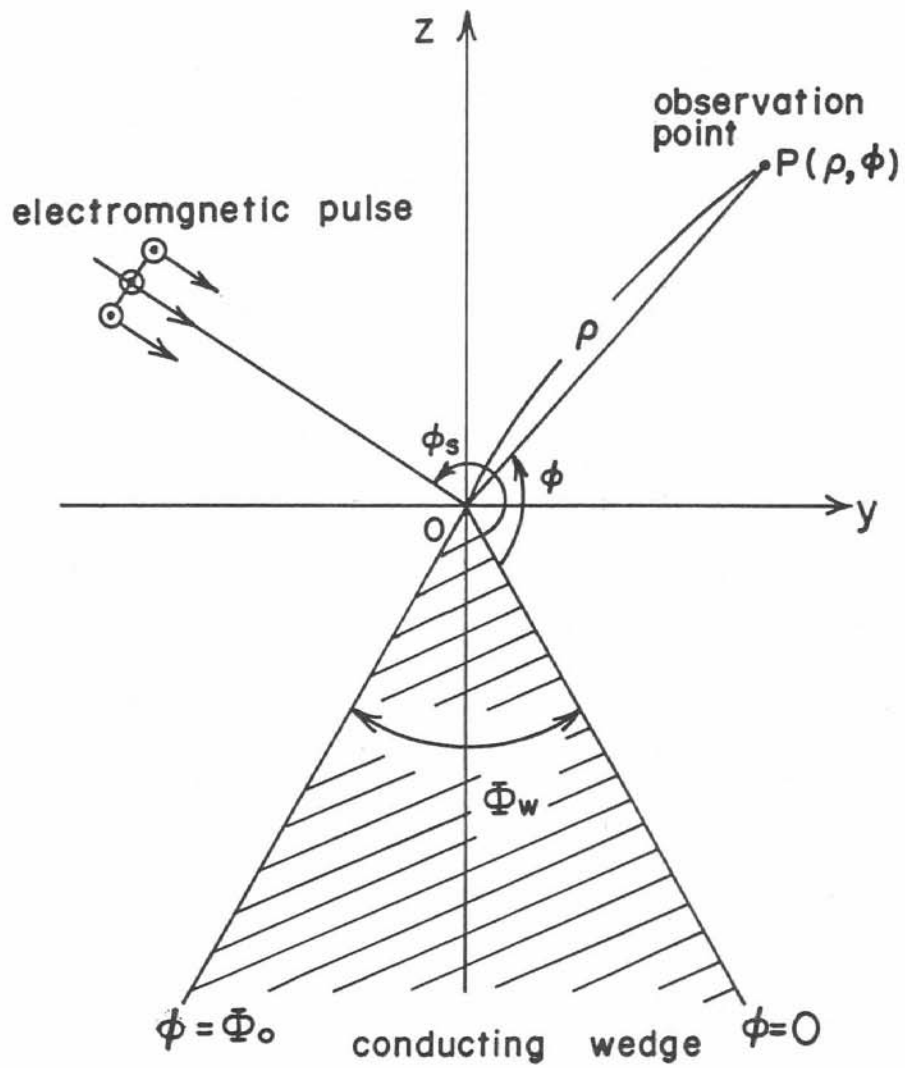


Fig.1 Geometry of the problem

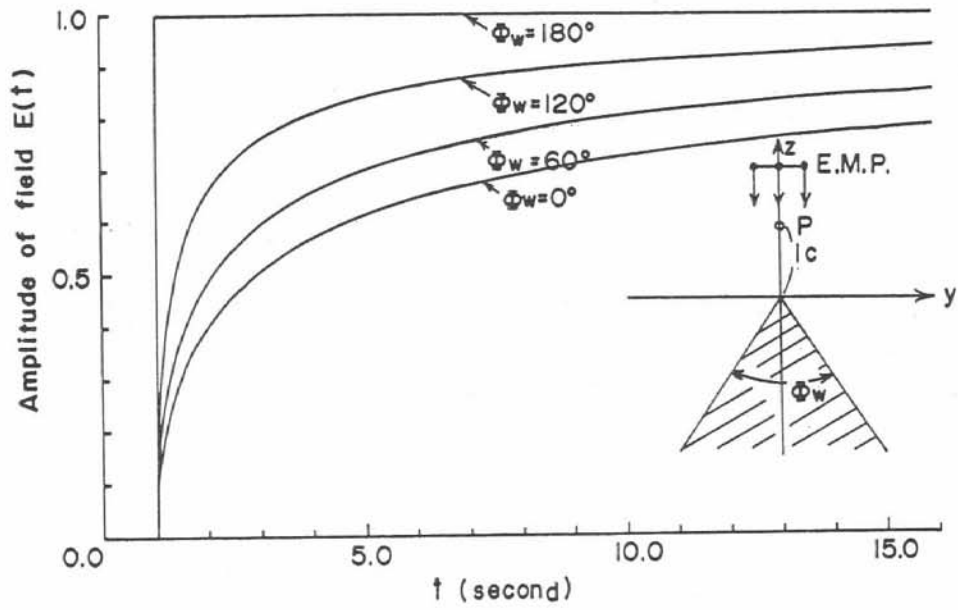


Fig.2(a) Time domain wave form for the step function

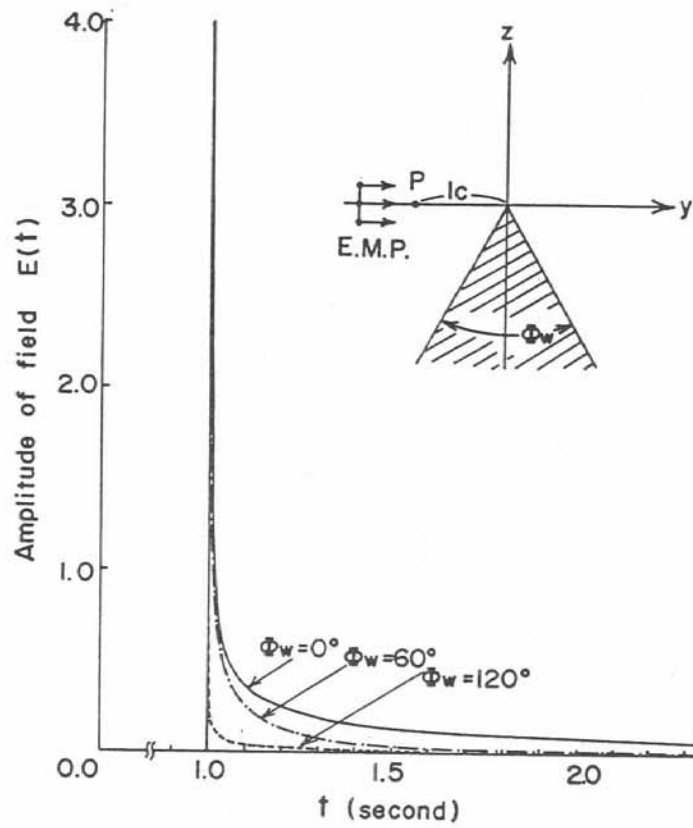


Fig.2(b) Time domain wave form for the delta function