

A Uniform Asymptotic Analysis for Transient Scattered Fields by a Cylindrically Curved Open Surface with Varying Radius of Curvature

#Keiji Goto, Toshihide Ajiki, Toru Kawano, and Toyohiko Ishihara
 Department of Communication Engineering, National Defense Academy
 Hashirimizu, Yokosuka, 239-8686 Japan
 E-mail: keigoto@nda.ac.jp

Abstract

The time-domain uniform asymptotic solution (TD-UAS) for the transient scattered field excited by the high-frequency (HF) pulse wave incident on a cylindrically curved open surface with a varying radius of curvature is presented in this paper. The TD-UAS, effective in the transition regions including the geometrical boundaries RB and SB, is constructed by the geometrical rays, the surface diffracted rays, the lowest order adiabatic whispering gallery mode radiation fields, and the combination of these pulse waves. The TD-UAS has an advantage that the total solution can be obtained from the summation of the individual solution which can easily be interpreted physically. We have confirmed the accuracy and the validity of the TD-UAS by comparing with the reference solution calculated from the combination of the method of moment (MoM) and the fast Fourier transform (FFT) code and with the reference solution obtained from the combination of the frequency-domain UAS and the FFT code.

1. INTRODUCTION

Recently, by the technological advances in high-resolution radar and electromagnetic pulses (EMP), it has become important to study the transient electromagnetic field radiated by an antenna or the transient scattered field produced by various objects [1], [2]. In the high-frequency (HF) analysis of the scattered field by an object with a complex shape, it is necessary to study the analysis method by an object with a relatively simple shape or the analysis method for the canonical problem [3]-[5].

The purpose of this paper is to derive the time-domain uniform asymptotic solution (TD-UAS) for the transient scattered field when the HF pulse wave is incident on a cylindrically curved open conducting surface with a varying radius of curvature. The accuracy and the validity of the TD-UAS proposed here are confirmed by comparing with the reference solutions calculated numerically from the combination of the frequency-domain (FD) numerical solution

obtained from the method of moment (MoM) [6], [7] and the fast Fourier transform (FFT) code and from the combination of the frequency-domain uniform asymptotic solution (FD-UAS) [8] and the FFT code.

2. FORMULATION

Fig.1 shows the cylindrically curved open conducting surface Ω with varying radius of curvature, the curved coordinate system (s, q) , the rectangular coordinate system (x, y, z) , and the coordinate system (R, ψ) . The origin of coordinate system (x, y, z) is chosen to coincide with the vertex point O of the curved surface Ω . Note that s and q in the coordinate system (s, q) are the distance along the curved surface measured from the point O and the vertical distance from the curved surface, respectively.

We assume that the radius of curvature $a(s)$ is sufficiently larger than the wavelength $\lambda (= 2\pi c/\omega)$ (ω and c are the

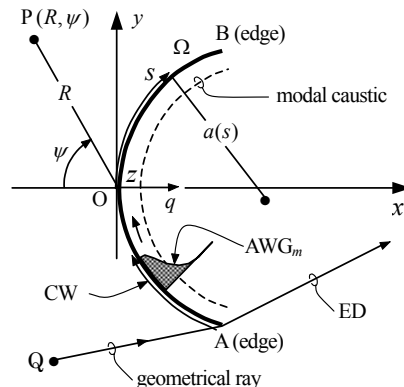


Fig.1 Cylindrically curved open conducting surface Ω with varying radius of curvature, coordinate systems (x, y, z) , (s, q) , and (R, ψ) . A, B: straight edges, Q: magnetic line source, P: observation point. Also shown are edge diffracted ray (ED), creeping wave (CW), and m th order adiabatic WG mode (AWG_m) excited by the geometrical ray (Q \rightarrow A) incident on the edge A.

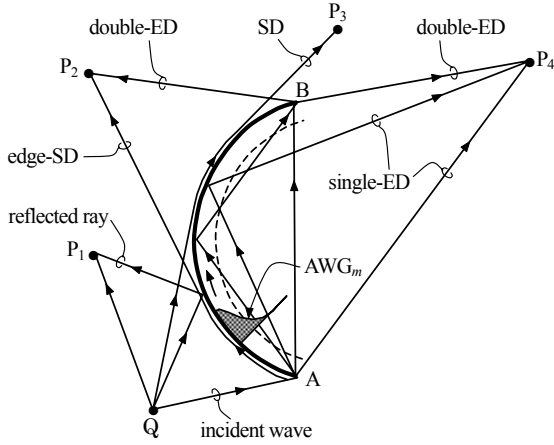


Fig.2 Single and double edge diffracted rays (single and double-ED), edge-surface diffracted rays (edge-SD) excited either by the edge A or both by the edges A and B. Also shown are geometrical rays (GO) including direct ray and reflected ray, and SD excited on the convex side by source Q.

radian frequency and the speed of light, respectively) i.e., $\omega a(s)/c \gg 1$, and the source Q and the observation point P (R, ψ) are located sufficiently away from the curved surface.

When the cylindrical wave emanated from the source Q is incident on the edge A of the curved surface Ω , the edge diffracted ray (ED), the creeping wave (CW), and the lower order m th order adiabatic WG mode (AWG_m) [9], [10] are excited in the respective regions (see Fig.1). These waves excited at the edge A propagate toward the edge B direction and become new incident waves on the edge B (see Fig.1). Fig.2 shows geometrically the scattering phenomena when the cylindrical wave is incident on the convex side of a cylindrically curved open conducting surface Ω with two edges A and B.

The transient scattered field solution $y(R, \psi, t) \equiv (y(t))$ can be obtained from the inverse Fourier transform of the product of the FD scattered field $u_d(\omega, R, \psi) \equiv (u_d(\omega))$ and the frequency spectrum $S(\omega)$ of the source function $s(t)$ as follows

$$y(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} u_d(\omega) S(\omega) \exp(-i\omega t) d\omega. \quad (1)$$

We will apply the Gaussian-type modulated pulse source $s(t)$ given by [2], [11], [12]

$$s(t) = \{U(t) - U(t - 2t_0)\} \cdot \exp\{-i\omega_0(t - t_0) - (t - t_0)^2 / (4d^2)\} \quad (2)$$

where $U(\bullet)$ is the unit step function and ω_0 is the central

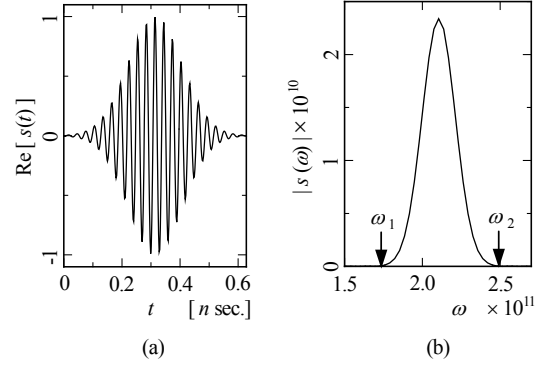


Fig.3 Gaussian-type modulated pulse source. (a) Real part of $s(t)$ in (2) with numerical parameters: $t_0 = 3.14 \times 10^{-10}$, $d = 6.60 \times 10^{-11}$, and $\omega_0 = 2.10 \times 10^{11}$. (b) Frequency spectrum $S(\omega)$ of the source function $s(t)$, and $\omega_1 \approx 1.76 \times 10^{11}$ and $\omega_2 \approx 2.45 \times 10^{11}$.

radian frequency modulating the pulse, and t_0 and d the constant parameters. The frequency spectrum $S(\omega)$ obtained by the Fourier transform of the source function $s(t)$ is given by

$$S(\omega) = 2d\sqrt{\pi} \exp\{i\omega t_0 - d^2(\omega - \omega_0)^2\} \text{Re}[\text{erf } \beta(\omega)] \quad (3)$$

$$\beta(\omega) = t_0 / (2d) - id(\omega - \omega_0) \quad (3a)$$

where $\text{Re}[\bullet]$ denotes the real part of $[\bullet]$. Fig.3 illustrates the source function $s(t)$ and its spectrum $S(\omega)$. The main portion of the frequency spectrum $S(\omega)$ is distributed in the HF domain approximately from $\omega = \omega_1$ to $\omega = \omega_2$, so that the integration interval in the inverse Fourier transform (1) can be changed from $(-\infty, \infty)$ to (ω_1, ω_2) (see Fig.3). Then, the FD scattered field $u_d(\omega)$ in (1) can be evaluated asymptotically under the HF assumption $\omega a(s)/c \gg 1$. The FD-UAS $u_{d,asy}(\omega)$ for $u_d(\omega)$ can be represented as follows [8]

$$u_d(\omega) \sim u_{d,asy}(\omega) = u_{d,1}(\omega) + u_{d,2}(\omega) + u_{d,WG,m}(\omega) \quad (4)$$

where $u_{d,1}(\omega)$ denotes the geometrical rays (GO) including the reflected ray and the ED, $u_{d,2}(\omega)$ the surface diffracted ray (SD) including the edge-SD, and $u_{d,WG,m}(\omega)$ the AWG_m radiation fields (see Fig.2).

After substituting the $u_{d,asy}(\omega)$ in (4) into $u_d(\omega)$ in (1), the integral $y(t)$ can be evaluated by applying the HF asymptotic analysis methods in 3. While, substituting the FD-numerical solution $u_{d,MoM}(\omega)$ obtained from the MoM into $u_d(\omega)$ in (1), one may obtain the numerical solution $y_{MoM}(\text{FFT})$ by applying the FFT code. The numerical solution $y_{MoM}(\text{FFT})$ thus obtained serves as the reference solution in 4.

3. TIME-DOMAIN UNIFORM ASYMPTOTIC SOLUTION

3.1 Uniform Asymptotic Analysis by Saddle Point Technique

In this section, we will derive the TD-UAS for the GO and the SD. First, let's take the single-ED (see Fig.4), emanated from the edge A and arriving at the observation point P₄ after reflecting once on the concave boundary, as a simple and good example of u_{d,1}(ω). Then the u_{d,1}(ω) can be represented as follows [8]

$$u_{d,1}(\omega) = G(QA)D_A(\omega, \phi_A, \phi_A^{in})G(AR) \cdot \sqrt{dA(R)/dA(P_4)} \exp(ikRP_4 - i\pi/2) \quad (5)$$

where G(x) denotes the 2-D Green's function

$$G(x) = \frac{i}{4} \sqrt{2c/\pi\omega x} \exp(i\omega x/c - i\pi/4) \quad (6)$$

and QA (AR) denotes the propagation distance of the ray traveling from the point Q (A) to the point A (R) (Henceforth, the distance between the point Q and A is indicated by QA). D_A(ω, φ_A, φ_Aⁱⁿ) is the edge diffraction coefficient for the observation angle φ_A and the incident angle φ_Aⁱⁿ and is given by

$$D_A(\omega, \phi_A, \phi_A^{in}) = -\frac{F(X^i)}{\cos \frac{\phi_A - \phi_A^{in}}{2}} - \frac{F(X^r)}{\cos \frac{\phi_A + \phi_A^{in}}{2}} \quad (7)$$

$$F(X) = -2i\sqrt{X} \exp(-iX) \int_{\sqrt{X}}^{\infty} \exp(i\tau^2) d\tau \quad (7a)$$

$$X^i = 2 \frac{\omega}{c} \frac{QA \cdot AR}{QA + AR} \cos^2 \frac{\phi_A - \phi_A^{in}}{2} \quad (7b)$$

$$X^r = 2 \frac{\omega}{c} \frac{AR \cdot \rho^\gamma}{AR + \rho^\gamma} \cos^2 \frac{\phi_A + \phi_A^{in}}{2} \quad (7c)$$

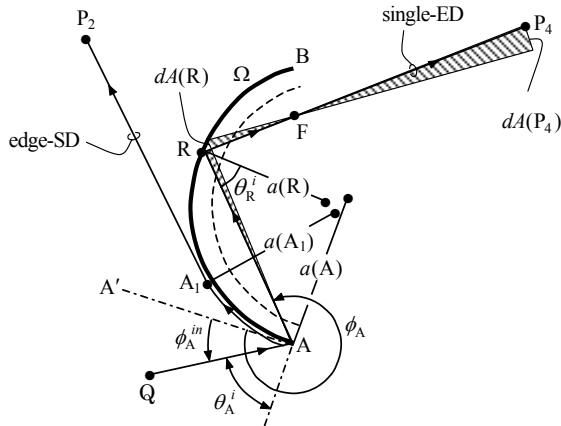


Fig.4 Single edge diffracted ray (single-ED) reflecting once on the concave boundary after the diffraction by the edge A and the edge surface diffracted ray (edge-SD).

$$\rho^\gamma = \frac{QA \cdot a(A) \cos \theta_A^{in}}{2QA + a(A) \cos \theta_A^{in}} \quad (7d)$$

In (5), $\sqrt{dA(R)/dA(P_4)} = \sqrt{RF/FP_4}$ denotes the divergence coefficient, dA(R) and dA(P₄) are the ray tube cross sections at R and P₄ (see Fig.4), respectively. RP₄ = (RF + FP₄) is the propagation distance from the reflection point R to P₄. (−π/2) phase shift arises from the caustic F. RF is given as follows

$$RF = \frac{AR \cdot a(R) \cos \theta_R^i}{2AR - a(R) \cos \theta_R^i} \quad (8)$$

where θ_Rⁱ and a(R) denote the incident angle and the radius of curvature at the point R, respectively.

The geometrical ray u_{d,1}(ω) in (5) can be expressed by

$$u_{d,1}(\omega) = A_1(\omega) \exp(i\omega L_1/c) \quad (9)$$

$$L_1 = Q \rightarrow A \rightarrow R \rightarrow P_4 \quad (9a)$$

where A₁(ω) is the slowly varying amplitude as the function of ω and L₁ denotes the propagation distance (see Fig.4) which is independent of ω.

Next, as an example of u_{d,2}(ω), we will consider the edge-SD propagating along the convex surface after the diffraction by the edge A (see Fig.4). This may be represented as [8]

$$u_{d,2}(\omega) = G(QA) \sum_{\ell=1}^{\infty} \left\{ D_A(\omega, \phi_\ell, \phi_A^{in}) \frac{L_\ell(A)}{2} T_\ell(A, A_1) \cdot D_\ell(A_1) \right\} G(A, P_2) \quad (10)$$

$$L_\ell(A) = (2\sigma_\ell)^{-1/2} (\omega a(A)/(2c))^{-1/6} \exp(i\pi/12) \quad (10a)$$

$$T_\ell(A, A_1) = \exp(i\omega \ell_1/(2c) - \Omega_\ell \ell_1), \quad \ell_1 = \int_A^{A_1} dt' \quad (10b)$$

$$\Omega_\ell \ell_1 = \sigma_\ell \exp(-i\pi/6) \int_A^{A_1} \frac{M(t')}{a(t')} dt' \quad (10c)$$

$$D_\ell(A_1) = \sqrt{2} (\omega a(A_1)/(2c))^{1/6} \frac{\exp(-i\pi/12)}{\sqrt{\sigma_\ell Ai(-\sigma_\ell)}} \quad (10d)$$

where φ_ℓ(v_ℓ = ka(A) cos φ_ℓ) denotes the eigen value of the ℓ th order CW satisfying the characteristic equation H_{v_ℓ}^{(1)'}(ka(A)) = 0. The notations L_ℓ(A), T_ℓ(A, A₁), and D_ℓ(A₁) are the launching coefficient from the edge A, the transmission coefficient from the edge A to the surface diffraction point A₁, and the surface diffraction coefficient at A₁, respectively (see Fig.4). The function Ai(•) is the Airy function [13]. u_{d,2}(ω) in (10) may be represented by the product of A₂(ω) and the phase term including the total propagation distance L₂ as follows:

$$u_{d,2}(\omega) = A_2(\omega) \exp(i\omega L_2/c) \quad (11)$$

$$L_2 = Q \rightarrow A \curvearrowright A_1 \rightarrow P \quad (11a)$$

The notation $A \curvearrowright A_1$ is used to indicate the CW propagation from A to A_1 along the arc of the curved surface Ω .

Substituting $u_{d,j}(\omega)$, $j=1,2$, in (9) or (11) and $S(\omega)$ in (3) into the inverse Fourier transform in (1) yields the following TD-integral representation

$$y_j(t) = \frac{d}{\sqrt{\pi}} s(t - L_j/c) I_j(\gamma), \quad j=1,2 \quad (12)$$

$$I_j(\gamma) = \frac{1}{2d^2} \int_{\omega'_1}^{\omega'_2} A_j(\omega'/(2d^2)) \text{Re}[\text{erf}\beta(\omega'/(2d^2))] \cdot \exp[-\gamma h_j(\omega')] d\omega' \quad (12a)$$

$$h_j(\omega') = [(\omega' - \omega'_0) + i(t - t_0 - L_j/c)]^2 \quad (12b)$$

$$\gamma = 1/(4d^2), \quad \omega'_0 = 2d^2\omega_0. \quad (12c)$$

In obtaining the above representations from (1), the transformation from ω to ω' via $\omega' = 2d^2\omega$ has been performed. Note that $\omega'_{1,2} = 2d^2\omega_{1,2}$.

For the large value of γ ($\gg 1$), the integral $I_j(\gamma)$ in (12a) can be evaluated asymptotically by applying the saddle point technique [11], [12], [14]. The result is given by

$$I_j(\gamma) \sim \frac{\sqrt{\pi}}{d} A_j\left(\frac{\omega'_{j,s}}{2d^2}\right) \text{Re}\left\{\text{erf}\beta\left[\frac{\omega'_{j,s}}{2d^2}\right]\right\} \quad (13)$$

where $\omega'_{j,s}$ is the saddle point :

$$\omega'_{j,s} = \omega'_0 - i(t - t_0 - L_j/c) \quad (13a)$$

in the complex ω' -plane determined from the saddle point equation $(\partial/\partial\omega') \cdot h_j(\omega') = 0$. Then substituting (13) into (12), the TD-UAS for the GO ($j=1$) and the SD ($j=2$) may be represented by

$$y_j(t) = A_j(\omega_{j,s}) \text{Re}[\text{erf}\beta(\omega_{j,s})] s(t - L_j/c) \quad (14)$$

$$\omega_{j,s} = \omega'_{j,s}/(2d^2) = \omega_0 - i(t - t_0 - L_j/c)/(2d^2). \quad (14a)$$

It is shown in (14) that the transient scattered field propagates with the phase velocity c and is observed after the total propagation time L_j/c .

3.2 Uniform Asymptotic Analysis by Fourier Transform Method

The solution $u_{d,WG,m}(\omega)$ in (4) for the m th order AWG $_m$ radiation field from aperture plane at the edge B can be inferred from the result given in [8], [9], [11] and be represented as follows

$$u_{d,WG,m}(\omega) = U(P)u_{m,go}(\omega) + u_{m,d}(\omega) \quad (15)$$

$$u_{m,go}(\omega) = G(QA)D_A(\omega, \phi_A, \phi_A^{in})G_{m,go}(\omega) = A_{m,go}(\omega) \exp(i\omega L_{m,go}(\omega)/c) \quad (15a)$$

$$u_{m,d}(\omega) = G(QA)D_A(\omega, \phi_A, \phi_A^{in})G_{m,d}(\omega) = A_{m,d}(\omega) \exp(i\omega L_{m,d}(\omega)/c) \quad (15b)$$

$$G_{m,go}(\omega) = G_m^i(R)\Gamma_h\sqrt{\text{RF}/\text{FP}} \exp(ikRP - i\pi/2) \quad (15c)$$

$$G_m^i(R) = M_{eq,m}(T_3)G(T_3R) \quad (15d)$$

$$M_{eq,m}(T_3) = G_m^r(\bar{R}) \exp(i\omega d'/c - i3\pi/4), \quad d' = \bar{R}T_3 \quad (15e)$$

$$G_m^r(\bar{R}) = \frac{K_m}{\sqrt{M(A)M(\bar{R})}} \frac{W_2(-\sigma_m)}{2} \exp\{i\omega T_0 \curvearrowright T_2/c\} \quad (15f)$$

$$K_m = i/\{4\sigma_m Ai(-\sigma_m)\}, \quad M(A) = (\omega a(A)/c)^{1/3} \quad (15g)$$

$$G_m^d(P) = u_m^i(B)D_B(\omega, \phi_B, \phi_B^{in})G(BP). \quad (15h)$$

Where $G(QA)$ and $D_A(\omega, w_m, w_{in})$ are the incident GO (see (6)) and the edge diffraction coefficient (see (7)), respectively, and $G_{m,go}(\omega)$ denotes the GO converted from the incident modal ray $G_m^i(R)$ and arriving at the observation point P. Therefore, $u_{m,go}(\omega)$ in (15a) denotes the GO (single-ED), converted from AWG $_m$ and arriving at the observation point P located in the illuminated region between RB_{WG} and SB_{WG} , with the total propagation

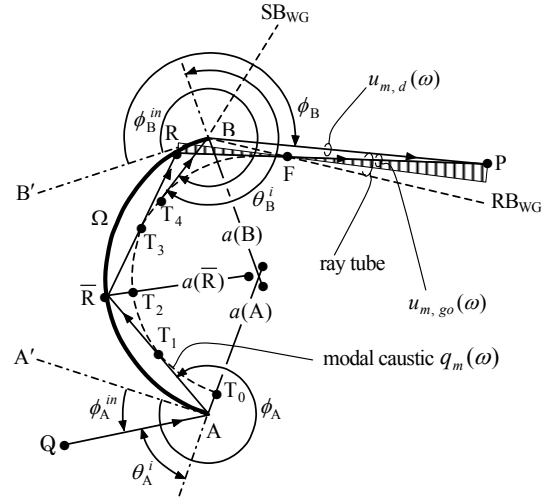


Fig.5 AWG $_m$ radiation field from the aperture plane at the edge B. The solution observed at P can be represented by the combination of geometrical ray (single-ED) and the edge diffracted ray (double-ED).

distance $L_{m,go}(\omega) (\approx Q \rightarrow A \rightarrow T_1 \curvearrowright T_3 \rightarrow R \rightarrow P)$ While, $u_{m,d}(\omega)$ in (15b) denotes the edge diffracted ray (double-ED), excited by the incident modal ray $G_m^i(B)$, with the total propagation distance $L_{m,d}(\omega) (\approx Q \rightarrow A \rightarrow T_1 \curvearrowright T_4 \rightarrow B \rightarrow P)$ (see Fig.5). The notation $T_1 \curvearrowright T_{3,4}$ denotes the AWG_m propagation from T_0 to $T_{3,4}$ along the arc of modal caustic defined by $q = q_m(\omega) = a(s) - \sigma_m(a(s)/2)^{1/3} \cdot (\omega/c)^{-2/3}$. Note that the total propagation distance $L_{m,j}(\omega)$, $j \equiv go$ or $j \equiv d$, changes as the function of ω .

$U(P)$ in (15) is “one” when the observation point is located in the illuminated region and “zero” when it is in the shadow region. Substituting $u_{m,j}(\omega)$ in (15a) and (15b) and $S(\omega)$ in (3) into (1) yields the following TD-integral representation for the AWG_m radiation field [11]

$$y_{m,j}(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} A_{m,j}(\omega) S(\omega) \exp[-i\omega\{t - L_{m,j}(\omega)/c\}] d\omega, \quad j \equiv go \text{ or } j \equiv d. \quad (16)$$

Since the total propagation distance $L_{m,j}(\omega)$ changes as the function of ω , it may be difficult to evaluate the integral $y_{m,j}(t)$ asymptotically by applying the saddle point technique. So, we will newly derive the uniform asymptotic solution, from the integral (16), by applying the Fourier transform method [11], [12].

The pulse source function $s(t)$ defined by (2) can be represented as follows

$$s(t) = \exp[-i\omega_0(t - t_0)] p(t) \quad (17a)$$

$$p(t) = \exp[-(t - t_0)^2 / (4d^2)]. \quad (17b)$$

Denoting the Fourier transform of $p(t)$ by $P(\omega)$, the frequency spectrum $S(\omega)$ in (3) can be represented as follows.

$$S(\omega) = \exp(i\omega_0 t_0) P(\omega - \omega_0) \quad (18)$$

$$P(\omega) = 2\sqrt{\pi} d \exp(i\omega t_0 - d^2 \omega^2) \text{Re}\{erf[\beta(\omega + \omega_0)]\} \quad (19)$$

Substituting (18) into (16) and evaluating the integral $y_{m,j}(t)$ in (16) by applying the Fourier transform method produce

$$y_{m,j}(t) = A_{m,j}(\omega_0) \exp[-i\omega_0(t - t_0 - L_{m,j}(\omega_0)/c) - (t - t_0 - L_{m,j}(\omega_0)/v_{g,m,j})^2 / (4d^2)] \quad (20)$$

$$v_{g,m,j} = c / (1 + \omega_0 L'_{m,j}(\omega_0) / L_{m,j}(\omega_0)). \quad (20a)$$

It is shown in (20) that the transient pulse wave for the AWG_m radiation field propagates with the phase velocity c and the group velocity $v_{g,m,j}$ given by (20a).

4. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we perform the numerical calculations necessary to assess the accuracy and the validity of the TD-

UAS derived in 3, and to interpret physically the phenomena of the transient scattered field. The pulse plane wave shown in Fig.3 is incident on the convex side of the cylindrically curved open surface Ω (see Fig.6) defined by

$$a(s) = 1 / (a_0 - a_1 |s|), \quad |s| \leq s_0 \quad (21)$$

where (a_0, a_1) are constant parameters and s_0 the arc length from the vertex point O to the edge A or B .

Fig.7(a) shows the real part of response waveform vs. time curves observed at $(R, \psi) = (0.8 \text{ m}, 100^\circ)$ (see Fig.1) when the pulse plane wave $s(t)$ is incident on the convex side of the curved surface Ω with the parameters $(a_0, a_1) = (10, 10)$ and $s_0 = 0.096$. The open circles ($\circ \circ \circ$: $y_{\text{MOM}}(\text{FFT})$) are the numerical reference solution. The solid curve (--- : $y_{\text{asy}}(\text{FFT})$) shows the numerical result obtained from the combination of the FD-UAS $u_{d,asy}(\omega)$ in (4) and the FFT code (see (1)). The solid curve agrees excellently with the reference solution in the whole region.

Although $y_{\text{MOM}}(\text{FFT})$ produces the numerical solution for the transient scattered field, it is difficult to separate each pulse individually from the total response waveform. While, $y_{\text{asy}}(\text{FFT})$ may be separated easily into each pulse, so that we shall use $y_{\text{asy}}(\text{FFT})$ as a new reference solution to assess the TD-UAS derived in 3 (see (14) and (20)). Fig.7(b) shows the pulses constituting the total response waveform in Fig.7(a). The closed circles ($\bullet \bullet \bullet$) show the result of each TD-UAS (see Fig.6). Reflected ray (①), single-ED (②, ③), double-ED (④ ~ ⑦), edge-SD (⑧), and AWG₁ radiation fields (⑨ and ⑩) agree very well with the new reference solution shown by the solid curve (---).

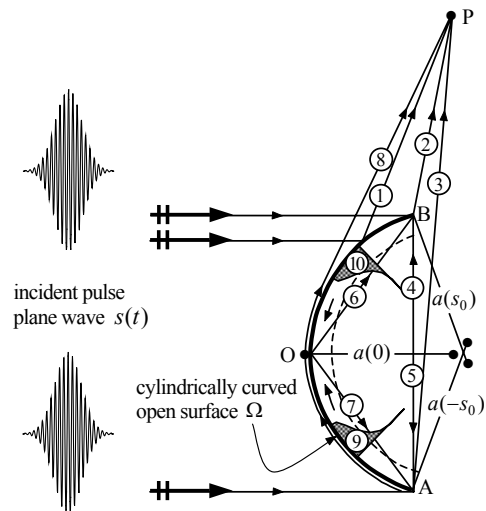


Fig.6 Scattered field observed at the point P. ①: reflected ray, ② and ③: single-ED, ④~ ⑦: double-ED, ⑧: edge-SD, ⑨ and ⑩: AWG₁ radiation fields.

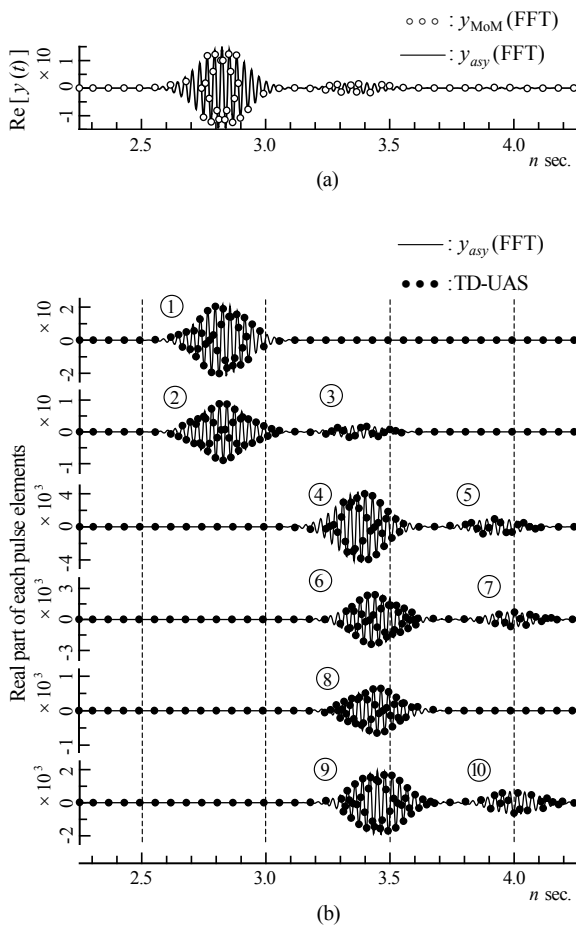


Fig.7 Total response waveform (Fig.7(a)) scattered by cylindrically curved open conducting surface and each pulse elements (Fig.7(b)). Numerical parameters: $(a_0, a_1) = (10, 10)$, $s_0 = 0.096$, and $(R, \psi) = (0.8m, 100^\circ)$.

5. CONCLUSION

We have derived the time-domain uniform asymptotic solution (TD-UAS) for the transient scattered field by the cylindrically curved open conducting surface with a varying radius of curvature. The TD-UAS consists of the geometrical rays including the reflected rays and the edge diffracted rays, the surface diffracted rays, and the lowest order WG mode radiation fields, and the combination of these pulse waves. The accuracy and the validity of the TD-UAS proposed here have been confirmed by comparing with the numerical reference solutions obtained from (i) the combination of the method of moment and the FFT code and (ii) the combination of the frequency-domain uniform asymptotic solution and the

FFT code. It has been shown that the TD-UAS is effective for physical interpretation of the scattered field since the pulses constituting the response waveform are observed separately.

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