PHASE DELAY AND ATTENUATION IN THE 50 TO 70 GHz BAND FOR ATMOSPHERIC PATH MODELS AT VARIOUS ALTITUDES\*

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The complex transfer function  $\tau$  of a clear atmosphere is dominated throughout the 40 to 80 GHz band by many (>43) molecular resonance lines of oxygen. The structure of  $\tau$  depends critically on the altitude h.

We present results of a computer analysis of attenuation and excess phase profiles due to  $0_2$  for horizontal  $(\alpha, \phi)$  and zenith (A,T) paths through the U.S. Std. Atm. 62. Known molecular constants, the Lorentzian line shape, and a semi-empirical model of line width were used. The constants of the width model, as determined by Carter et al. from fits of extensive attenuation measurements taken a various altitudes, form the basis for our results.

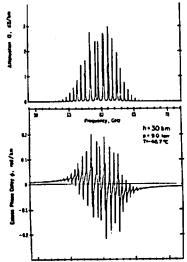


Fig. 1 - Well-resolved atmospheric oxygen spectrum for a horizontal path model at h = 30 km.

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## HORIZONTAL (homogeneous) PATHS

The attenuation per unit distance is given by2  $\alpha = [(4\pi f/c) \ 10 \log e] n''(f), dB/km,$ the excess phase per unit distance is  $\phi = (2\pi f/c) \Delta n'(f)$ , rad/km; where f-frequency, c-speed of light. n''(f) (extinction spectrum) and  $\Delta n'$  (f) (dispersion of refractive index) were evaluated as the sum of the first 43  $0^{18}_{2}$  lines. Fig. 1 shows at h = 30 km the individual lines fairly well isolated, while at h = 0km all lines have merged to one broad line (Fig. 2). Fig. 2 shows differences in  $\alpha$  and  $\phi$  that result from discrepancies in the width parameter (same for all lines) obtained from fits of field (666 MHz) and of Artman's Laboratory<sup>3</sup> (968 MHz) data.

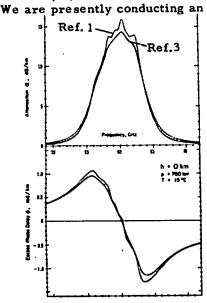


Fig. 2 - Atmospheric transmission response at sea level (U. S. Std. Atm. 62)

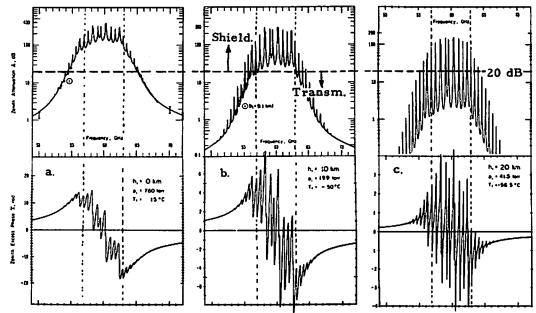


Fig. 3 - Total attenuation and excess phase delay due to atmospheric oxygen for zenith paths from different initial altitudes, h, to outer space.

extensive experimental program to establish reliable values for  $\alpha$  and  $\phi$  over the full meteorological range of p and T using a pressure-scanning ( $\Delta$ n' and n'') spectrometer.

## ZENITH PATHS

The zenith attenuation if given by:  $A = \int_{h_i}^{\infty} [a(h) d h]$ , in dB; and the integrated excess phase is:  $T = \int_{h_i}^{\infty} [\phi(h) d h]$ , in rad.

The integration was performed numerically using Simpson's rule and dividing the U.S. Std. Atm. 62 into 151 layers ( $\Delta p \le 10$  torr) from the initial altitude, hi=0 up to 80km. The calculation is quite involved requiring, e.g., for Fig. 3a about 3.9×10<sup>7</sup> individual computations for 1000 frequency steps. Three examples are given in Fig. 3.

More complete results and a detailed discussion are being published.<sup>4</sup>

## <u>APPLICATIONS</u>

The spectrum between 57 and 63 GHz offers one feature not found at any lower frequency: High attenuation and phase delay rates related to the fairly stable (compared to  $H_2$ 0 density fluctuations) dry part of the atmosphere. This

effords shielding of satellite-satellite links against ground interferences and restricted-range (secure) communication systems.

However, the shielding properties break down as a jammer gains altitude. If we arbitrarily assume a medium loss of 20 dB to separate shielding (+dB) from transmission (-dB), we find from  $h_i = 0 \text{km}, \geq +85 \text{dB}, \text{ from } h_i = 10 \text{km},$  $\geq$ +10 dB. At hi = 15 km 8 propagation channels (bandwidths 0.3 to 0.5 GHz) open up (≤ - 12 dB). Transmission increases to  $\leq -18/-19.5$  dB for h<sub>i</sub>=20/25 km. Tin the pass band of these 8 channels varies roughly between  $\mp 5$  to  $\mp 3$  radians (see Fig. 3).4 Differential phase measurements between two points are also of interest to gain absolute integrated dry term refractivity for correction of e.m. distance measurements.

## REFERENCES

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- 2. Liebe, IEEE Trans. AP-17, 621, 1969.
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