

## Optimum circular-coverage gain of multimode horns with specified peak cross-polarization and sidelobe levels

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### 1 Introduction

Dual mode horns [1] and choked horns [2] can be used as an antenna for circularly covering a wide area. However, it is difficult to control radiation property like directivity synthesis in reflector antennas, in which sidelobe level due to the sub-reflector was optimized based on quadratic programming approach [3]. In this paper, we demonstrate that an optimum circular-coverage gain of multimode horns with specified peak cross-polarization and sidelobe levels can be presented by using the quadratic programming approach. The gain of the horns is numerically evaluated by comparing with uniformly illuminated gain.

### 2 Formulas for quadratic programming

Since an aperture distribution of an axially symmetrical horn can be expanded by multiple  $TE_{1n}$  and  $TM_{1m}$  modes, its universal radiation pattern for circular polarization is obtained by linear combination of radiation pattern  $f_{k,i}(u)$  ( $k = 1, 2$ ) of  $i$ -th mode with coefficient  $c_i$  normalized by an equal power, where  $u = D/\lambda \sin \theta$ ,  $D$  is the aperture diameter and  $k = 1$  or  $2$  denote co-polar or cross-polar components, respectively. The gain is also given by  $G_k(u) = 4\pi|F_k(u)|^2/P_t$  ( $k = 1, 2$ ), where  $P_t$  is total power. Hence, for maximizing the gain  $G_1(u)$  over a circular coverage  $0 \leq u \leq u_e$  with specified sidelobe level  $|R|$  and peak cross-polarization level  $|X|$  (see Fig. 1), we now consider an optimization maximizing  $G_1(u_e)$  subject to  $F_1(u_e) = 1$  and

$$F_1(u) \geq 1 \quad (0 \leq u \leq u_e) \quad (1)$$

$$-R \leq F_1(u) \leq R \quad (u_0 \leq u \leq u_s) \quad (2)$$

$$-X \leq F_2(u) \leq X \quad (0 \leq u \leq u_x) \quad (3)$$

with

$$F_k(u) = \sum_i c_i f_{k,i}(u) \quad (k = 1, 2), \quad G_1(u_e) = 4\pi/P_t, \quad P_t = \sum_i c_i^2. \quad (4)$$

Where  $u_e$  denotes the edge of the coverage, and  $u_0 \leq u \leq u_s$  denotes the sidelobe region. When the aperture distribution of the conical horn is represented by superposition of cylindrical waveguide modes,  $f_{k,i}(u)$  in the far-field region is given by the real function [4]. Therefore the real coefficient  $c_i$  of each mode is solved by minimizing the quadratic objective function  $P_t$  subject to the linear equality/inequality constraints based on the quadratic programming approach. The mode coefficient  $C_i$  for the multimode horns excited by unit power is finally determined by  $C_i = c_i/\sqrt{P_t}$ .

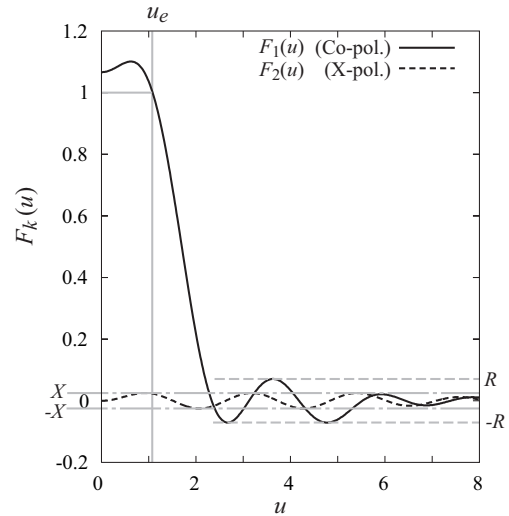


Fig. 1. Parameters for quadratic programming.

### 3 Numerical results and evaluation

Figure 2 (a) shows the aperture distributions of circularly polarized multimode horns with maximum gain over the circular area, where  $r$  denotes the coordinate in radius direction at the aperture. These distributions are illustrated for various parameters of  $u_e (= D/\lambda \sin \theta_e)$ , where  $\theta_e$  denotes the direction at the edge of the circular coverage. Figure 2 (b) also shows various universal patterns radiated by the aperture distributions in Fig. 2 (a). These patterns are normalized by the peak gain due to the uniform aperture distribution. Figures 3 (a) and (b) show excitation coefficients of cylindrical  $TE_{1n}$  and  $TM_{1m}$  modes at the aperture of the horn as shown in Fig. 2, respectively. These results are obtained by the quadratic programming for each parameter  $u_e$ .

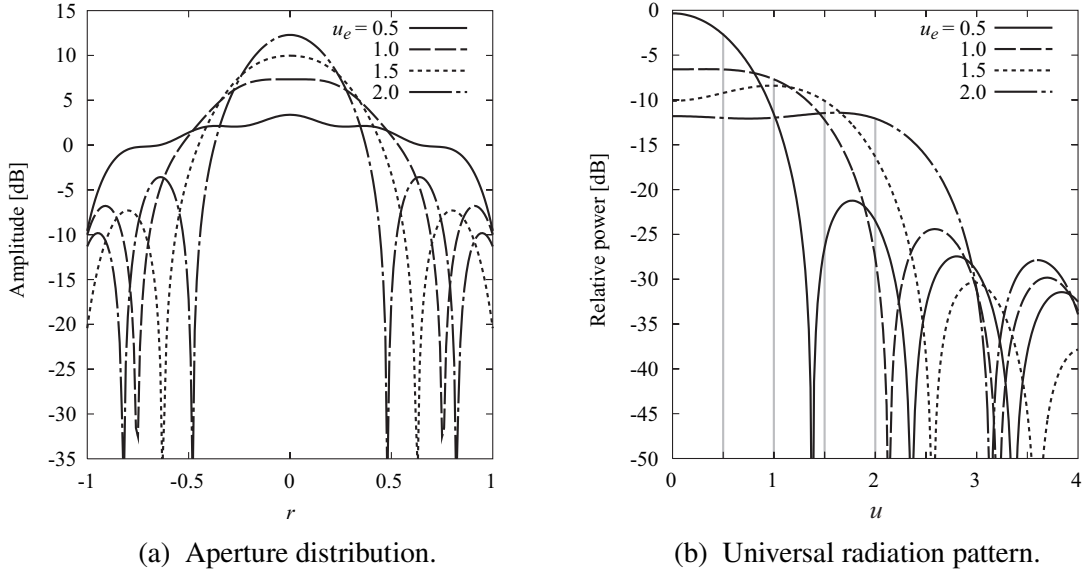


Fig. 2. Field distribution of multimode horns for covering circular area.

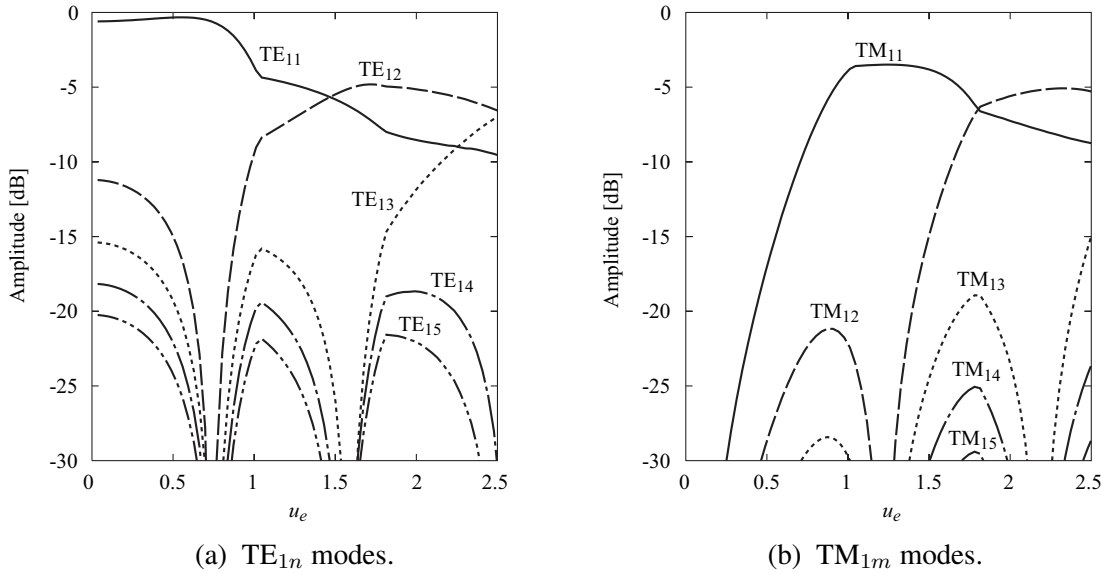


Fig. 3. Cylindrical mode coefficients of multimode horns for covering circular area.

Figure 4 (a) shows the relative gain ( $\theta_e \ll 1$ ) at  $u = u_e$  normalized by the gain at  $u = 0$  and also shows  $\Delta G_v$  to evaluate capability of the horns with modes in Fig. 3.  $\Delta G_v = G_v - G_i$  [dB] is defined by an ideal gain  $G_i$  [dBi] when the coverage is uniformly illuminated, and the minimum gain  $G_v = G_1(u_e)$

[dBi] over the circular coverage [5]. As shown in Fig. 4 (a),  $\Delta G_v$  becomes higher as the diameter  $D/\lambda$  increases. However, in the horns with about  $u_e < 0.5$ , its aperture diameter is too small to obtain the desired beamwidth similar to a simple horn. On the other hand, Fig. 4 (b) shows the peak level of the cross-polarization component together with the first sidelobe level. It is found that these levels take periodically the local minima depending on the parameter  $u_e$ . The aperture diameter  $D/\lambda$  minimizing the cross polarization component is determined from null points  $u_e \simeq 0.77, 1.53$  and  $2.47$ . Especially, the first null point is produced by first two modes as shown in Fig. 3 (a), so it corresponds to dual-mode horns. On the contrary, the horns with  $u_e \simeq 1.04$  and  $1.81$  have peak values of these levels. Thus, we have performed the optimization to suppress the peak cross-polarization level.

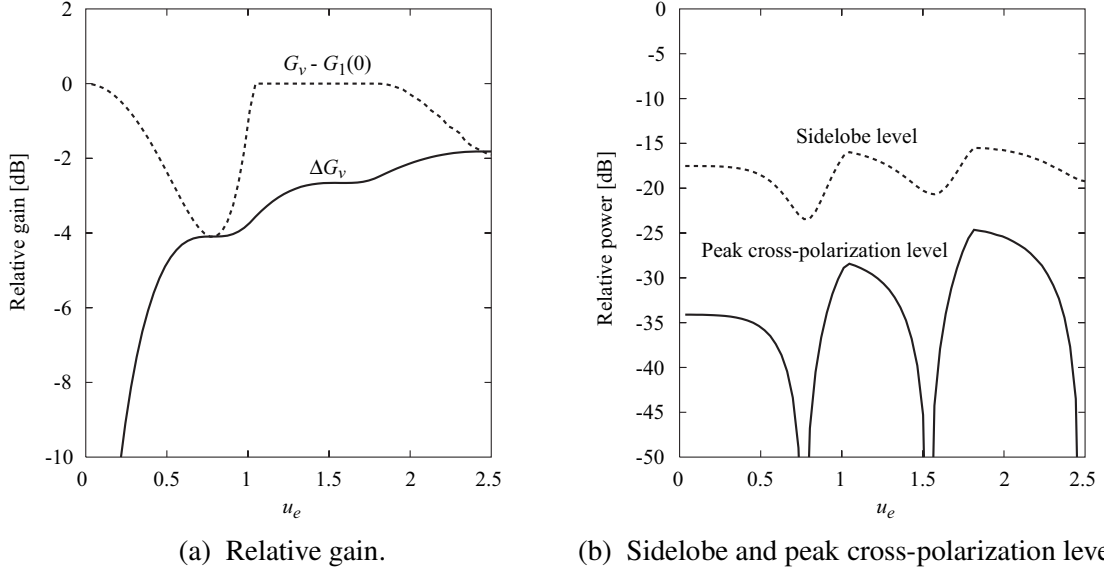


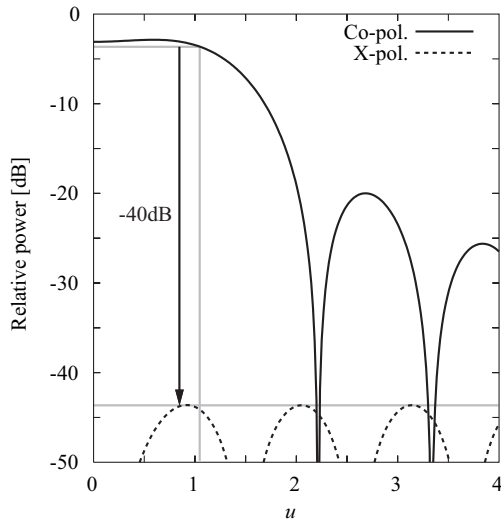
Fig. 4. Radiation characteristics of multimode horns optimized for covering circular area.

Figure 5 (a) shows the co- and cross-polarization components of the universal pattern excited by a circular polarization in the case of  $u_e = 1.04$ , and the specified cross-polarization level is  $-40$  dB. It is confirmed from Fig. 5 (b) that rotationally symmetrical co-polar field is achieved by sufficiently suppressing the cross-polarization component. In this case,  $\Delta G_v$  is  $-3.6$  dB and the first sidelobe level is  $-16.9$  dB. Furthermore, we have optimized the radiation patterns to achieve the low sidelobe level less than  $-30$  dB. Figures 6 (a) and (b) show the aperture distribution and the universal pattern, respectively, including the comparison between the linear and circular polarization for  $u_e = 1.53$ . The  $\Delta G_v$  is  $-2.7$  dB, the first sidelobe level is  $-30$  dB and also the cross-polarization level is less than  $-50$  dB.

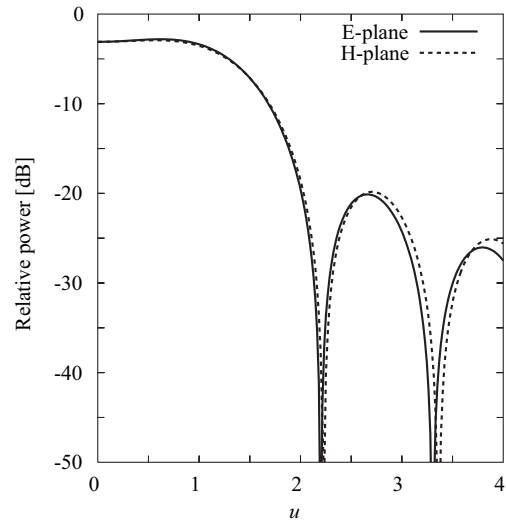
#### 4 Conclusions

The optimum circular-coverage gain of the multimode horns with specified peak cross-polarization and sidelobe levels has been solved by the optimization based on the quadratic programming approach. The detail discussion for the capability to cover circular area will be presented at the talk.

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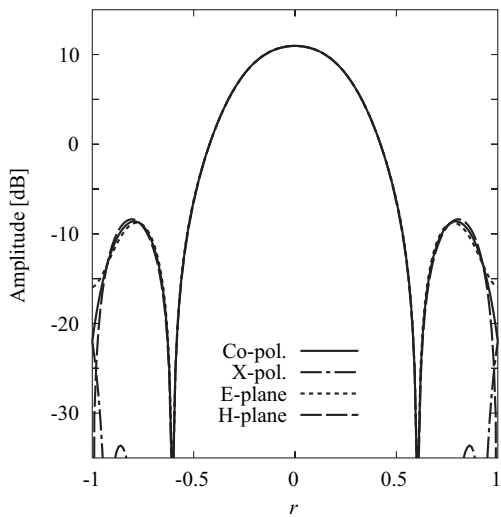


(a) Circular polarization.

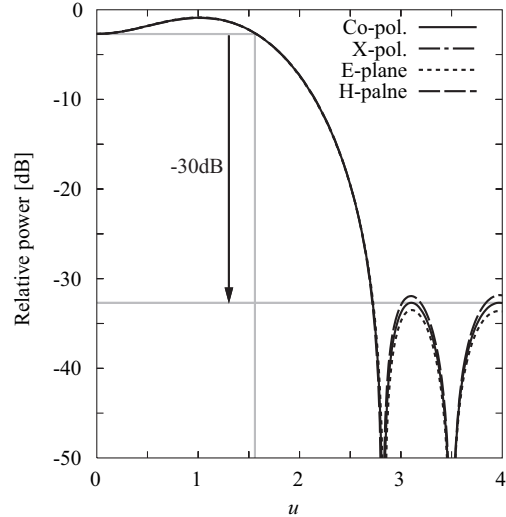


(b) Linear polarization.

Fig. 5. Universal radiation pattern with low cross polarization less than  $-40$  dB for  $u_e = 1.04$ .



(a) Aperture distribution.



(b) Universal radiation pattern.

Fig. 6. Low cross-polarization horn with specified sidelobe level for  $u_e = 1.53$ .

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