# RCS Measurement and PO Simulation of a Scale Model Rocket 

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## 1. Introduction

The simple RCS measurements are well-known as the near-field method to obtain the farfield RCS conversion [1], and the compact range method with the reflector [2] and the phasehologram range [3] for the scaled sized model target. The authors have investigated the scale model measurement and the Method of Moment (MoM) simulation with the Multi Level Fast Multi-pole Method (MLFMM) [4]. In this paper, the scale model measurement method in an anechoic chamber with 4.4 m long and the physical optics (PO) simulation are presented. The simulation methods are compared for simulating the RCS of the scale model rocket. The measurement environment is examined in detail to reduce the mutual coupling between the transmitting and receiving antennas. The measured and simulated RCS results are compared with the theoretical values of the scale model rocket.

## 2. Simulation Methods

Fig. 1 shows the photograph of the scale model rocket made of aluminium. The model consist of 3 parts; cone, cylinder and hemisphere. The longitudinal length of the model is 78 cm . The joint part between the cylinder and the cone is covered by a copper tape in order to reduce the influence of the gap. The analysis frequency of 10 GHz is employed and the longitudinal length is corresponding to $26 \lambda$. Table 1 shows simulation methods for electromagnetic analysis of RCS. The commercial simulator FEKO Suite 5.3 is used for the analysis. In the case of Method of Moment (MoM), the Multi Level Fast Multi-pole Method (MLFMM) is applied to reduce calculation memory and time. However, the calculations cannot reach to appropriate convergence (residuum is less than 0.003 ). And the calculate time is about 2 hours per a direction with the iteration of 500 times. In the case of Physical Optics (PO) simulation, even though it can be applied for a smooth surface, the requirement of memory size and the calculate time is very low. In the simulation of the model, the memory and the calculate time are 70 MB and less than 10 seconds, respectively.

Fig. 2 shows the simulated RCS results obtained by MLFMM and PO simulations. The simulated region is around the tip of the cone part. The RCS of the MLFMM results is about 5 dB higher than that of PO simulation. Considering the insufficient convergence of MLFMM and the smooth surface of the model, PO simulation is employed as the analysis method.

## 3. Measurement Environment

Fig. 3(a) shows the configuration of the transmitting and the receiving antennas for the measurement of RCS. The separation length between the corner reflector antennas is 17 cm . The reduction of mutual coupling between the transmitting and the receiving antenna is important in the measurement. The antennas are covered with the corned shape absorbers, and the absorber plate with 3 cm thickness is arranged between the antennas. The received power $P_{r}$ can be obtained by

$$
\begin{equation*}
P_{r}=P_{t}+G_{s t}+G_{s r}-L_{s p a c e}-L_{a b s} . \tag{1}
\end{equation*}
$$

Here, $P_{t}$ is the transmitted power, $G_{s t}$ and $G_{s r}$ are the antenna gain of the transmitting and receiving antennas in a direction to each other, $L_{\text {space }}$ is the propagation loss, and $L_{\text {abs }}$ is the loss of the absorbers. From this configuration, the mutual coupling of -90.8 dBm is achieved. Fig. 3(b) and (c) show the environment of the turn table. The turn table can not be ignored as a reflection object under the measurement of such minute values and increases a noise level as show in Fig. 3 (b). The reflection can be suppressed by placing absorbers in front of and on the turn table. The noise level
of -75.8 dBm is achieved and it is corresponding to a measurement condition of a circular disk of $r=2 \mathrm{~cm}$.

Fig. 4 shows a RCS pattern of a circular disk of $r=2 \mathrm{~cm}$. Because the difference between the peak and the noise level is 10 dB , the reflection wave of the disk can be observed accurately.

Fig. 5 shows the relation of the received level $P_{r}[\mathrm{dBm}]$ and theoretical RCS [dBsm] of circular disks of $r=2,5$ and 10 cm . The received levels $P_{r}$ are plotted as the triangles with reference of the left axis. The theoretical RCS values $\sigma$ are obtained by Eq. (2) and are plotted as the squares with the reference of the right axis. Because the tendencies of received levels and theoretical RCS are same, the measured results are considered to be proper. The relation of $\sigma$ and $P_{r}$ at $r=2 \mathrm{~cm}$, the following transform equation is obtained.

$$
\begin{equation*}
\sigma=P_{r}+43 \tag{3}
\end{equation*}
$$

From the noise level of $-75.8 \mathrm{dBm}, \sigma$ of over 32.8 dBsm can be measured. And the equation is ensured by Friss's formula and cable losses.

## 4. Measured and Simulated Results of the Scale Model Rocket

Fig. 6 shows the RCS pattern of measured and PO simulation results the rocket model. And theoretical RCS values of tip (Eq.(4)), cylinder (Eq.(5)) and hemisphere (Eq.(6)) are also shown. In hemisphere RCS (radiation angle of $180^{\circ}$ ), measured and simulated results and theoretical values agree very well. And angular region of $110^{\circ}$ to $250^{\circ}$, measured and simulated results agree very well. In cylinder RCS (radiation angle of $90^{\circ}$ and $270^{\circ}$ ), the measured results are about 4.5 dB less than the simulated results and theoretical value. It is due to that the measurement distance of 4.4 m is not sufficient for the far field of the frequency of 10 GHz and the model length of $26 \lambda$. In tip RCS (radiation angle of $0^{\circ}$ ), the differences among the measured and the simulated results and the theoretical value are observed. The measurement alignment and PO simulation of the tip are left as future challenges.

In order to compare the measured and simulated results in detail, both results from $0^{\circ}$ to $50^{\circ}$ and from $120^{\circ}$ to $180^{\circ}$ are shown in Fig. 7 (a) and (b). In Fig. 7 (a), from $0^{\circ}$ to $20^{\circ}$, the cycle and peak level of the measured and the simulated results agree well. And from $30^{\circ}$ to $50^{\circ}$, upper tendency of both results agree well. Fig. 7 (b), the measured and simulated results agree very well.

## 5. Conclusions

Measured and simulated results of RCS characteristics of the scale model rocket are obtained and compared with the theoretical values. Important results are summarized in the following;
(1) For electromagnetic analysis of RCS of the rocket model, PO simulation is effective and the results agree with the measured results and theoretical values.
(2) Exact measurement of RCS over -32.8 dBsm in an anechoic chamber is obtained.

## References

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Fig. 1 Scale Model Rocket
Table 1 Simulation Methods

|  | memory $_{\text {(//direction) }}$ | time (/1direction) | usefulness |
| :--- | :--- | :--- | :--- |
| MoM <br> (Method of Moment) <br> with MLFMM | 1.5 GB | 2 hour | Maximum number of iterations <br> are exceed without convergence. |
| PO <br> (Physical Optics) | 70 MB | less than <br> 10 sec | Only smooth surface can be <br> applied. |

[dBsm]


Fig. 2 Compared with PO and MLFMM


Fig. 3 Measuring Equipments


Fig. 4 Disk Radiation Pattern(r=2cm)

Circular Disk RCS : $\sigma=\frac{4 \pi\left(\pi r^{2}\right)^{2}}{\lambda^{2}}$ Eq.


Fig. 5 Relations of $\mathrm{P}_{\mathrm{r}}$ and $\sigma$


Fig. 6 Comparing RCS Result

(a) $0-50 \mathrm{deg}$

(b) 120-180 deg

Fig. 7 Comparing RCS Result

